

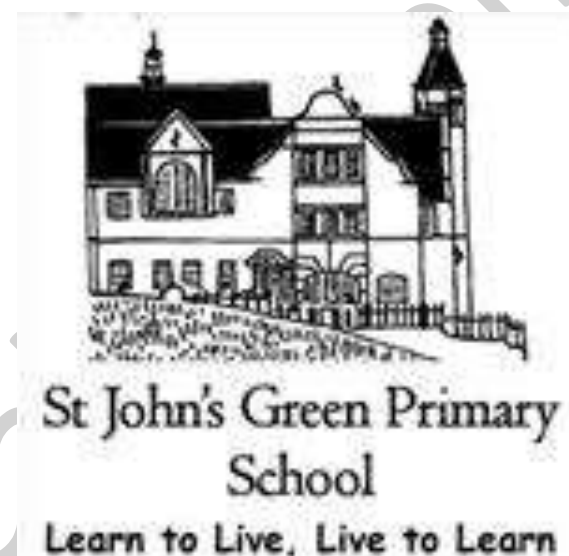
Calculation policy

Rationale

The aim of this document is to provide information on how our school promotes conceptual understanding through a concrete-pictorial-abstract approach. The policy documents a consistent approach using the concrete manipulatives readily available at St John's Green Primary. It also ensures consistency and progression in calculation methods.

Teachers should examine the methods of the previous year group as well as their current class when designing lessons.

The school welcomes a use of a range of manipulatives; however, teachers should refer to this document as starting point for planning learning.



'If learners do not use concrete materials, they cannot understand the mathematics. If they only use concrete materials, they are not doing mathematics'

Gu (2015)

Year 1 Addition

Using Place value

Count in ones / Counting in tens, e.g. knowing $45 + 1$ or $45 + 10$ without counting on in ones

$$23 + 10$$

1	2	3	4	5	6	7	8
11	12	13	14	15	16	17	18
21	22	23	24	25	26	27	
31	32	33	34	35	36	37	

Counting on

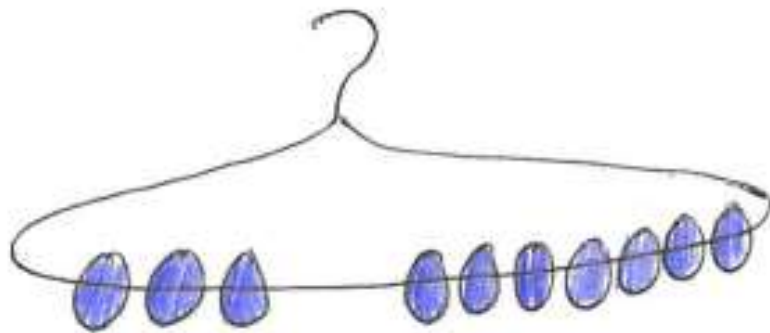
Count on in ones, e.g. $11 + 2 =$ $7 + 4 =$

Count on in tens, e.g. $45 + 20$ as 45, 55, 65

Using number facts

'Story' of 4, 5, 6, 7, 8 and 9, e.g. $7 = 7 + 0$ or $6 + 1$ or $5 + 2$ or $4 + 3$

Number bonds to 10, e.g. $5 + 5$, $6 + 4$, $7 + 3$, $8 + 2$, $9 + 1$, $10 + 0$



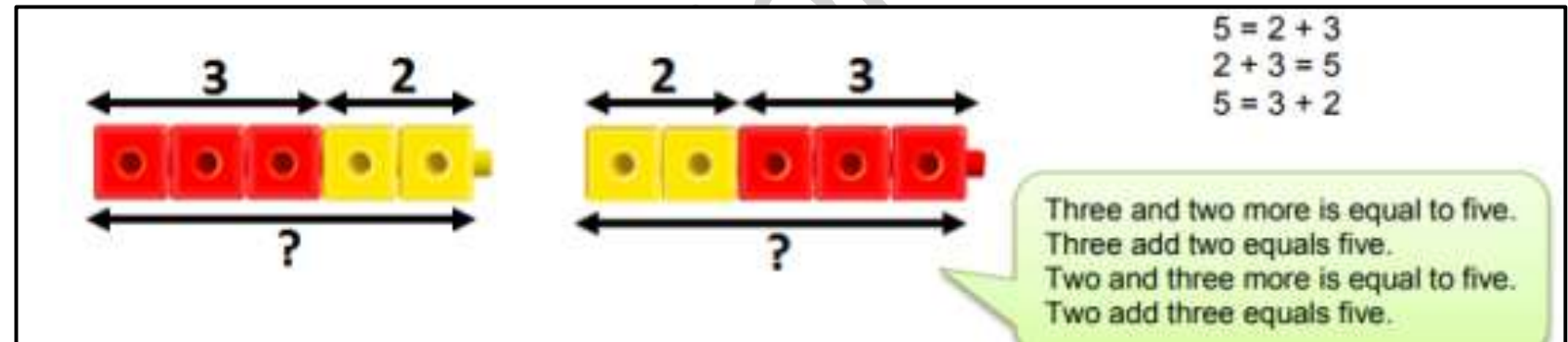
Patterns using known facts, e.g. $4 + 3 = 7$ so we know $24 + 3$, $44 + 3$, $74 + 3$, etc.

We would also expect year 1 children to have some experience creating groups of ones, using straws or sticks (bundling)

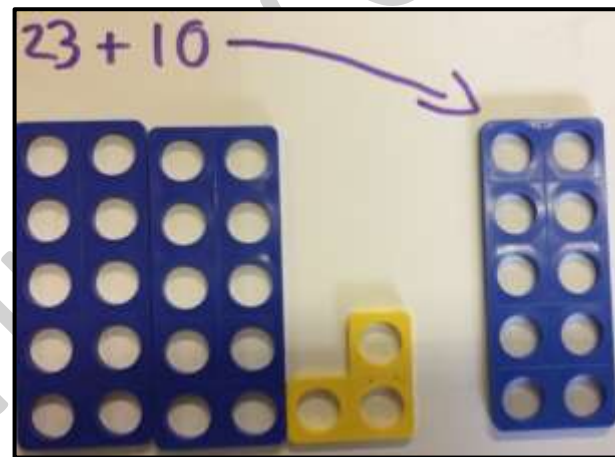
$$10 = 10 \text{ ones} = 1 \text{ ten}$$



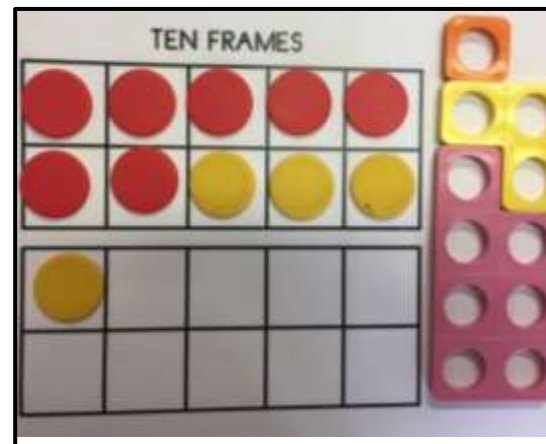
Understanding the relationship between addition and subtraction



Adding 10 to number



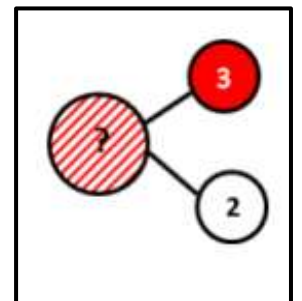
$$11 + 4 = 11 + 3 + 1$$



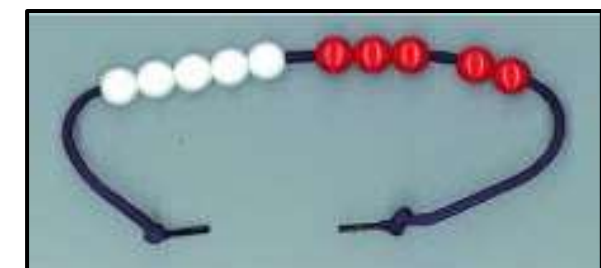
The story of 7



Part - whole model. Objects used as well as numerals



What is 2 more than 3?



Year 1 Subtraction

Using Place value

Count back in ones / Count back in tens, e.g. knowing $53 - 1$ or $53 - 10$ without counting back in ones

$$33 - 10$$

1	2	3	4	5	6
11	12	13	14	15	16
21	22	23	24	25	26
31	32	33	34	35	

Taking away

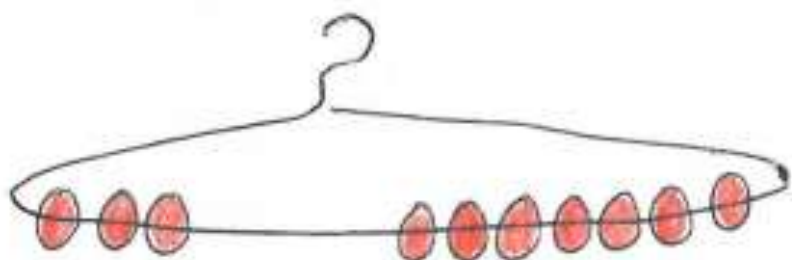
Count back in ones, e.g. $11 - 3 =$ $15 - 4 =$

Count back in tens, e.g. $53 - 20$ as 53, 43, 33

Using number facts

'Story' of 4, 5, 6, 7, 8 and 9, e.g. $7 - 1 = 6$, $7 - 2 = 5$, $7 - 3 = 4$, etc.

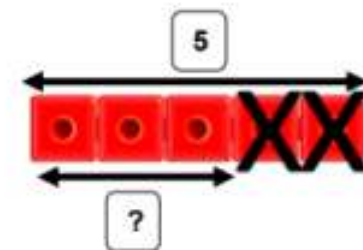
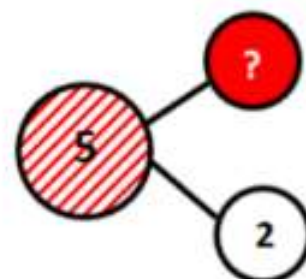
Number bonds to 10, e.g. $10 - 1 = 9$, $10 - 2 = 8$, $10 - 3 = 7$, etc.



Patterns using known facts, e.g. $7 - 3 = 4$ so we know $27 - 3 =$, $47 - 3 =$, $77 - 4 =$, etc.

Take away (One quantity is decreased by a provided amount)

Five sweets were on the table. Tom ate two sweets. How many sweets are on the table now?



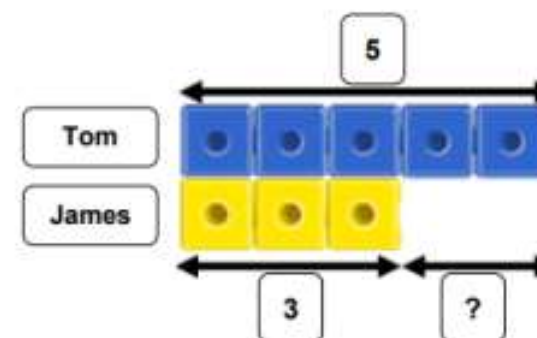
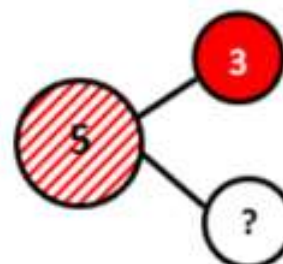
$$5 - 2 = 3$$

$$3 = 5 - 2$$

Two fewer than five is three.
Three is two fewer than five.

Comparison (Find the difference) *Key model showing the relationship between addition and subtraction

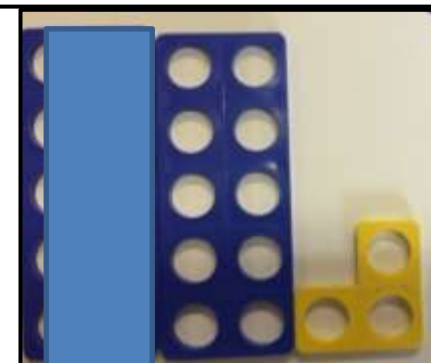
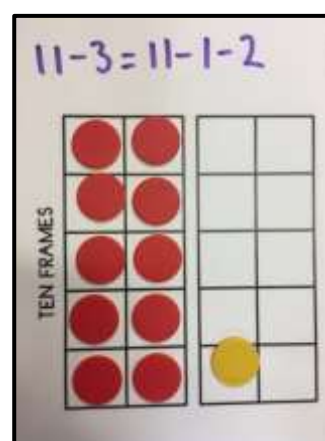
Tom has five sweets and James has three sweets. How many more sweets does Tom have than James?



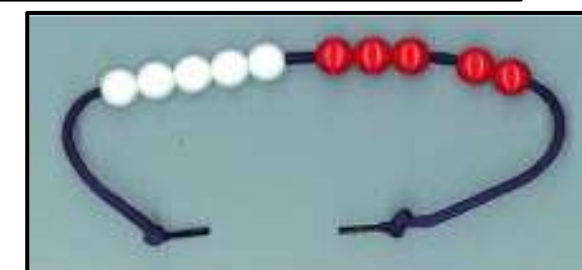
$$5 - 3 = 2$$

$$2 = 5 - 3$$

Five is two more than three.
Three is two fewer than five.



$$23 - 10$$



5 count back 2

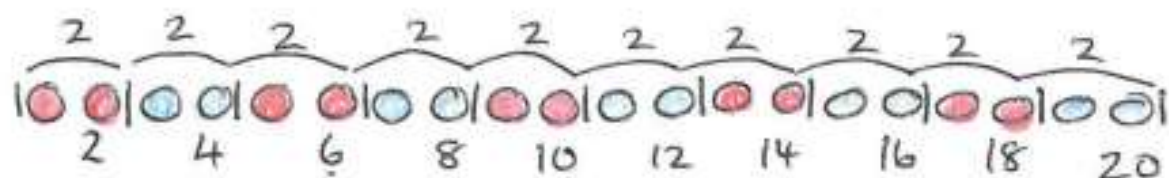
5-1
5-2
5-3 etc Subtraction covers may also be used



Year 1 Multiplication

Counting in steps ('Clever' counting)

Count in 2s and 10s



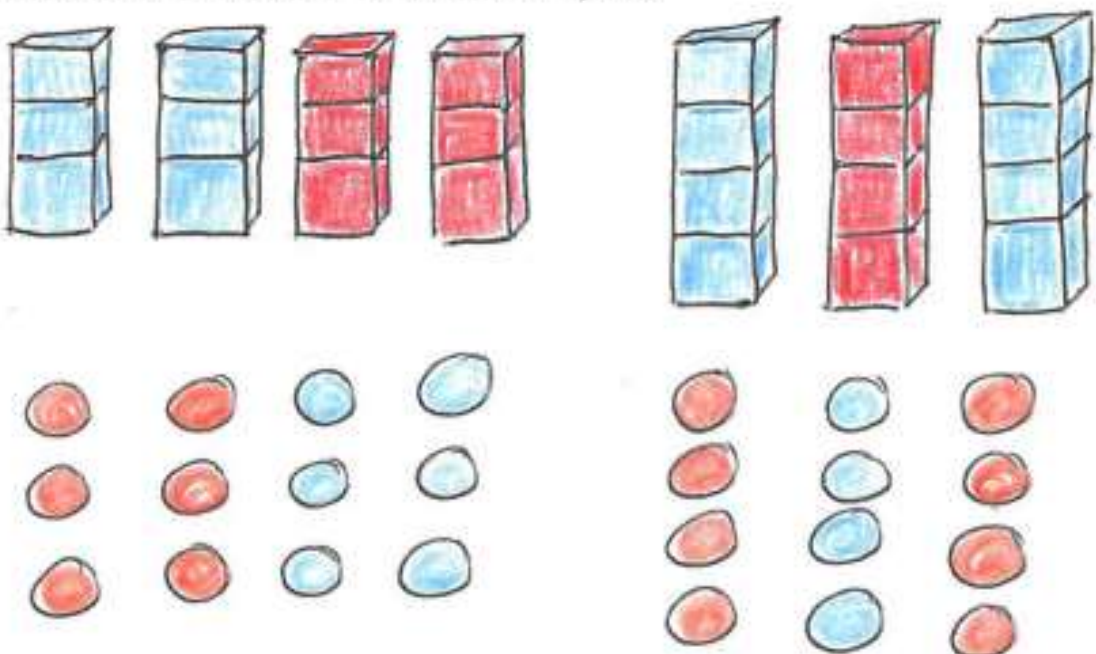
Doubling and halving

Find doubles to double 6 using fingers

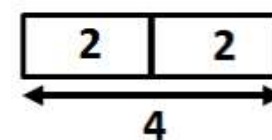


Grouping

Begin to use visual and concrete arrays and 'sets of' objects to find the answers to '3 lots of 4' or '2 lots of 5', etc.



Doubling and halving

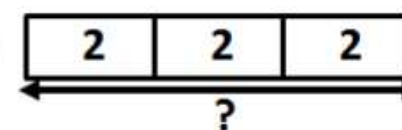


Two and two makes four.
Double two is equal to four.
Half of four is two.

$$\begin{aligned} 2 + 2 &= 4 \\ 2 \times 2 &= 4 \\ 4 - 2 - 2 &= 0 \\ 4 \div 2 &= 2 \end{aligned}$$

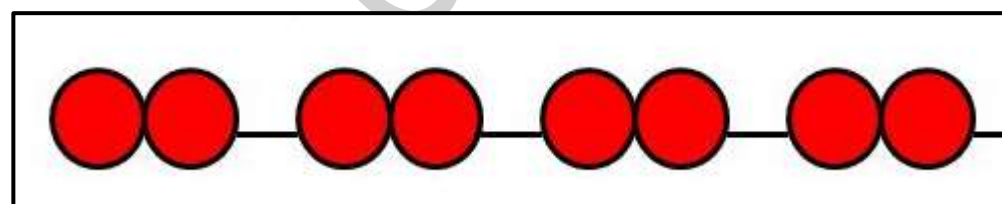
Multiplication – Equal groups

Amber wants to give her three friends two lollies each. How many lollies does she need?

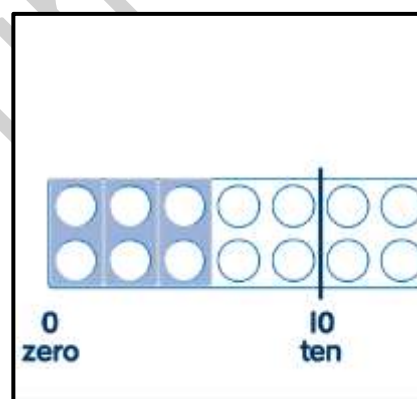


Two and two and two makes six.
Three groups of two make six.

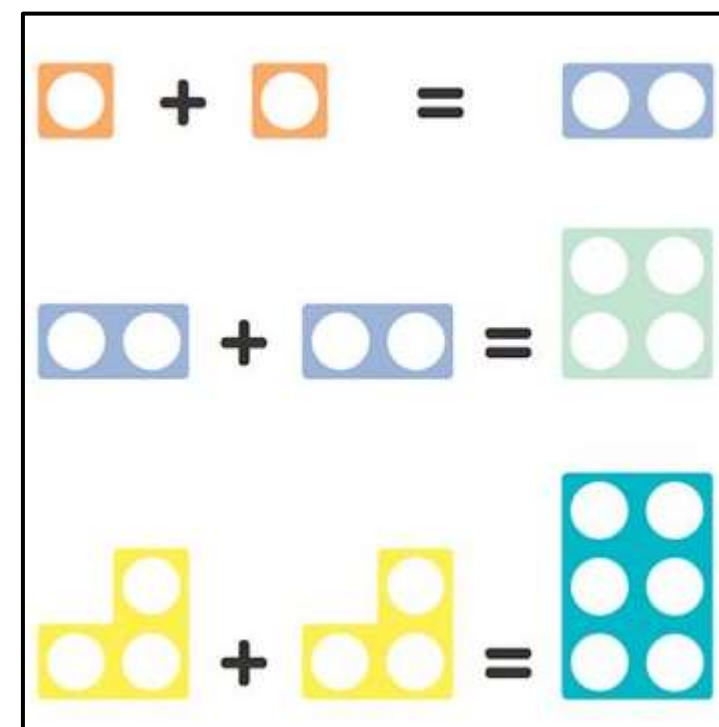
$$\begin{aligned} 2 + 2 + 2 &= 6 \\ 3 \times 2 &= 6 \end{aligned}$$



Counting in 2s on a beadstring



3 groups of 2 with a number line

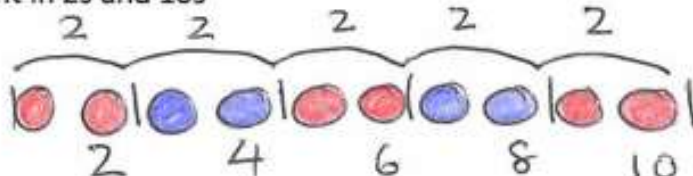


Knowing all doubles to double 6

Year 1 Division

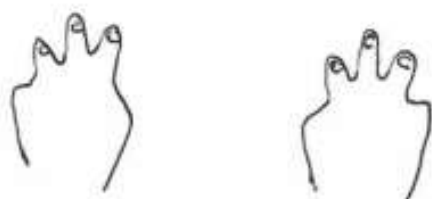
Counting in steps ('Clever' counting)

Count in 2s and 10s



Doubling and halving

Find half of even numbers up to 12 including realising that it is hard to halve an odd number

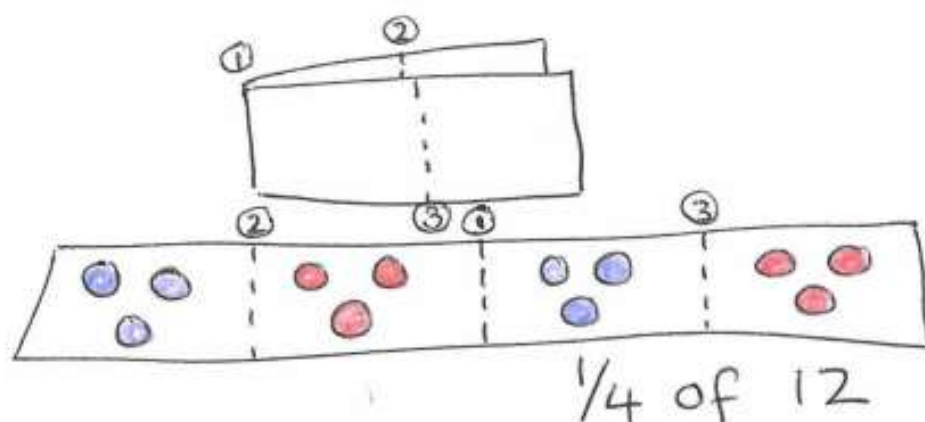


Grouping

Begin to use visual and concrete arrays and 'sets of' objects to find the answers to 'how many towers of 3 can I make with 12 cubes?'

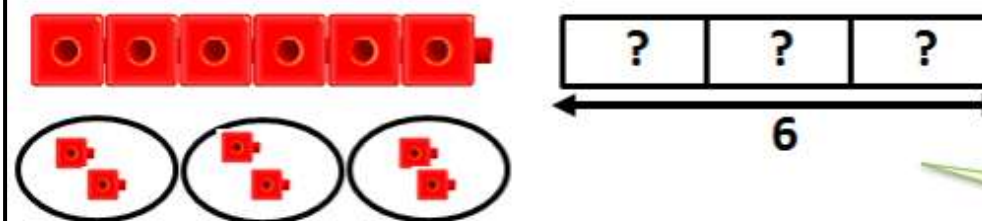
Sharing

Begin to find half of a quantity using sharing, e.g. half of 16 cubes by giving one each repeatedly to two children



Division – Sharing

Amber has six lollies. She wants to share them equally between her three friends. How many lollies does each of her friends get?

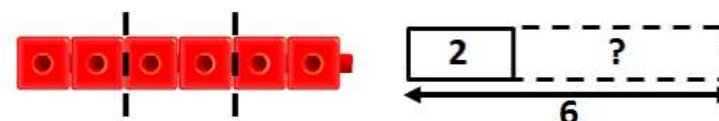


$$6 \div 3 = 2$$

Six shared into three equal groups is two in each group.

Division – Grouping

Amber has six lollies. She wants to give each of her friends two lollies. How many friends can she give lollies to?



$$6 \div 2 = 3$$

Six grouped into twos equals three

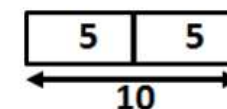
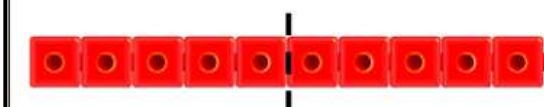
Fractions

- Recognise, find and name a half as one of two equal parts of an object, shape or quantity
- Recognise, find and name a quarter as one of four equal parts of an object, shape or quantity

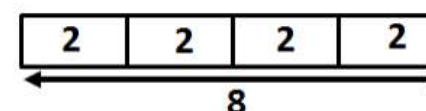
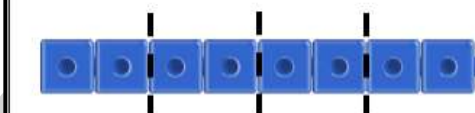
Cuisenaire rods can be used to explore generalisation in fractions.



Orange is double the yellow.
Yellow is half of the orange.
Yellow add yellow equals orange.
Orange subtract yellow equals orange.



Four reds are equal to brown.
A quarter of brown is one red.
Red add red add red add red equals brown.



How many sets of 2 make 6?



Finding half of even numbers



Children should have experience of creating tens by grouping straws/cubes/sticks

Year 2 Addition

Using Place value

Know 1 more or 10 more than any number, e.g. 1 more than 67 or 10 more than 85

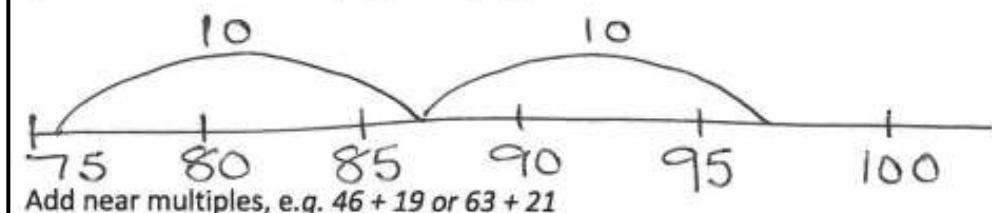
Partitioning, e.g. $55 + 37$ as $50 + 30$ and $5 + 7$ finally combining the two totals: $80 + 12$

$$\begin{array}{r} 50 \\ + 30 \\ \hline 80 \end{array} \quad \begin{array}{r} 5 \\ + 7 \\ \hline 12 \end{array} \quad \begin{array}{r} 80 \\ + 12 \\ \hline 92 \end{array}$$

Counting on

Add ten and multiples of ten, e.g. $76 + 20$ as 76, 86, 96 or in one hop $76 + 20$

Add two 2-digit numbers by counting on in tens then in ones, e.g. $55 + 37$ as 55 add 30 (85) add 7 (92)

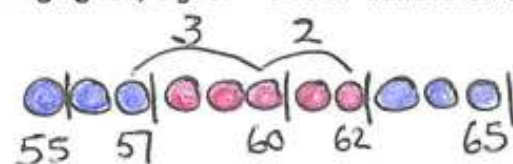


Using number facts

Know pairs of numbers which make the numbers up to and including 10, e.g. $8 = 4 + 4$, $3 + 5$, $2 + 6$, $1 + 7$ and $10 = 5 + 5$, $4 + 6$, $3 + 7$, $2 + 8$, $1 + 9$, $0 + 10$

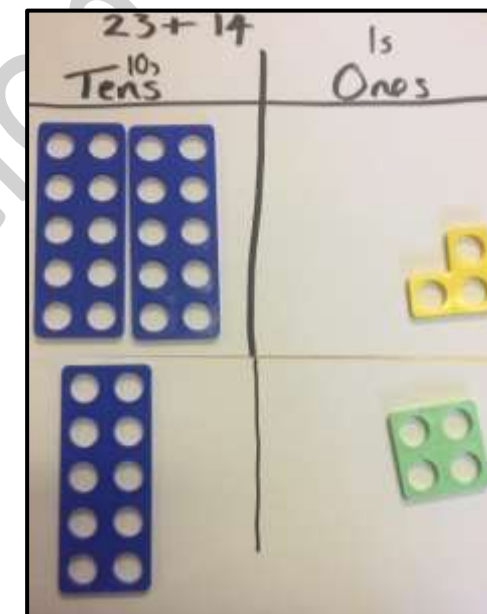
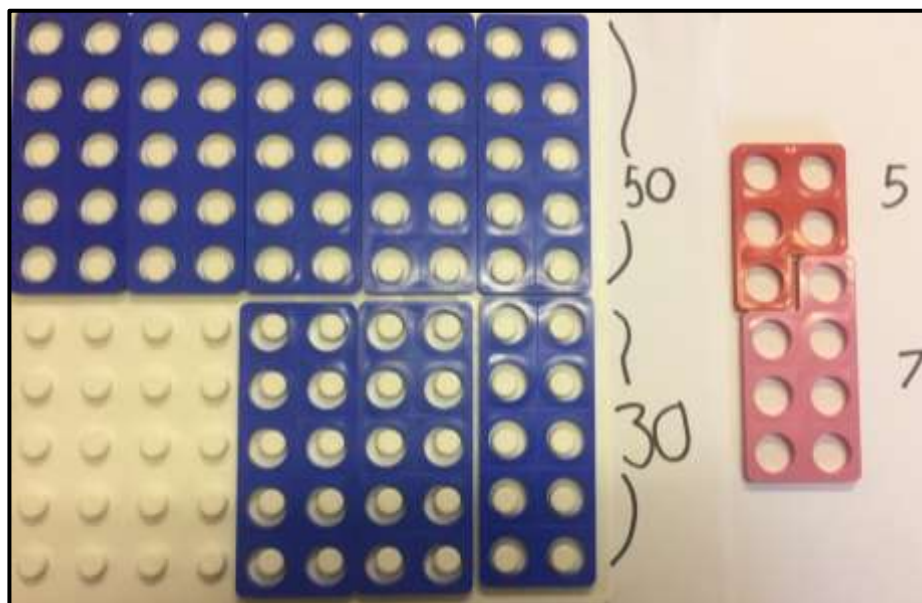
Patterns of known facts, e.g. $6 + 3 = 9$, so we know $36 + 3 = 39$, $66 + 3 = 69$, $53 + 6 = 59$

Bridging ten, e.g. $57 + 5$ as 57 add 3 then add 2 more



Adding three or more single-digit numbers, spotting bonds to 10 or doubles, e.g. $6 + 7 + 4 + 2$ as $10 + 7 + 2$

Partitioning into tens and ones to add



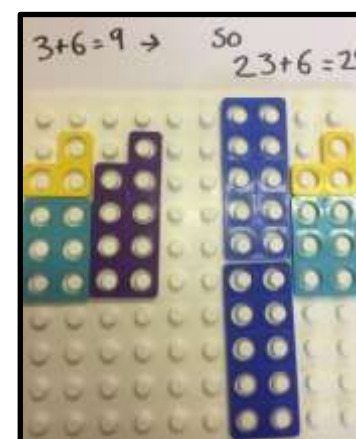
Understanding the relationship between addition and subtraction

$$\begin{array}{l} 9 = 3 + 6 \\ 9 = 6 + 3 \\ 9 - 6 = 3 \\ 9 - 3 = 6 \end{array}$$

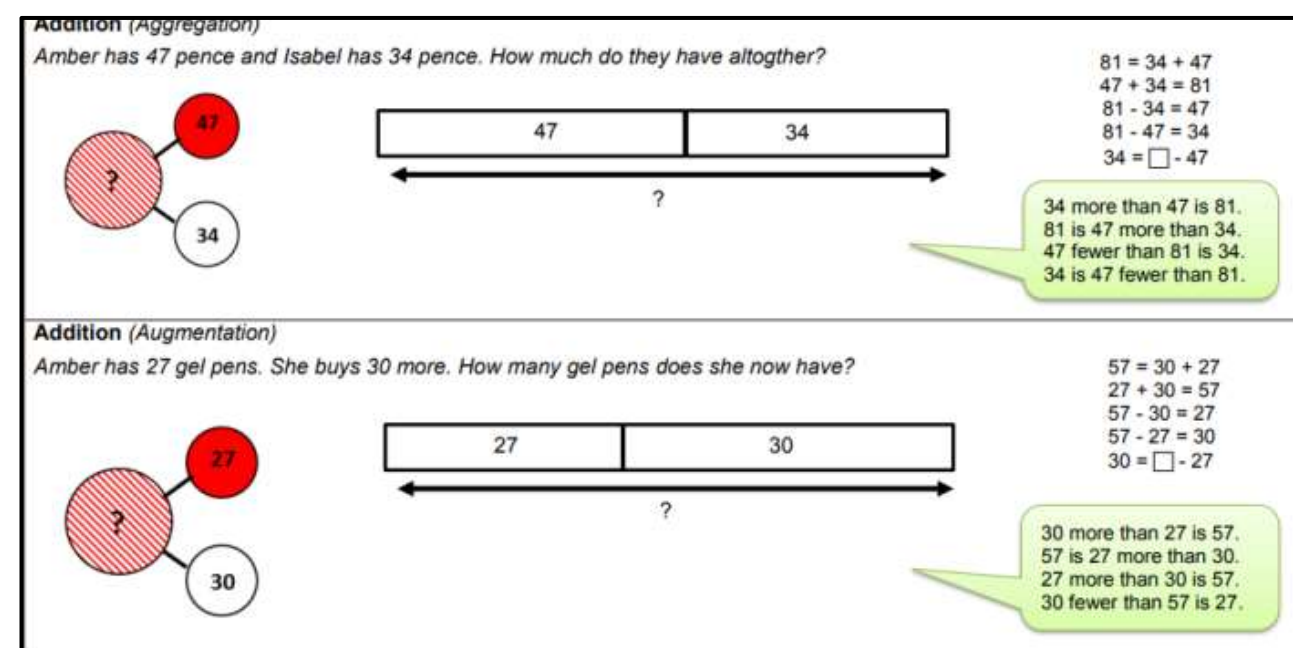
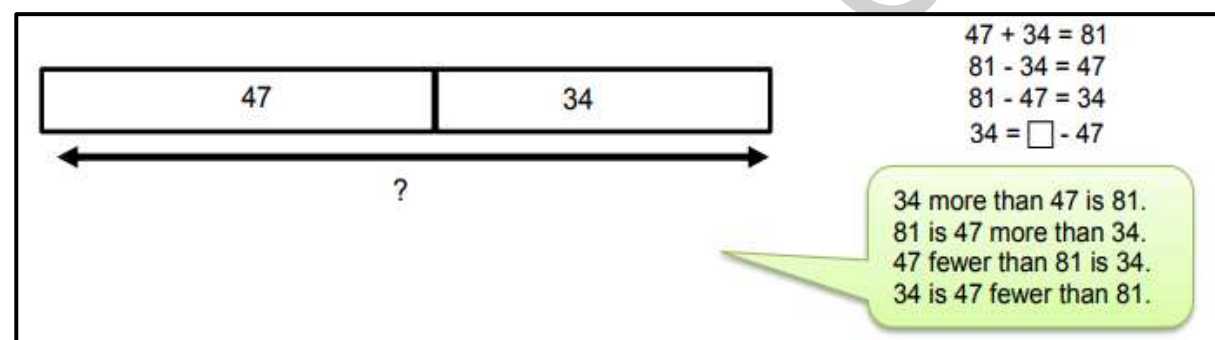
Knowing addition facts



Patterns of known facts



Using addition facts to fill and bridge ten



Year 2 Subtraction

Using Place value

Know 1 less or 10 less than any number, e.g. 1 less than 74 or 10 less than 82
Partitioning, e.g. $55 - 32$ as $50 - 30$ and $5 - 2$ combining the answers: $20 + 3$

$$\begin{array}{r} 50 \\ - 30 \\ \hline 20 \end{array} \quad \begin{array}{r} 5 \\ - 2 \\ \hline 3 \end{array} \quad \begin{array}{r} 20 \\ + 3 \\ \hline 23 \end{array}$$

Taking away

Subtract ten and multiples of ten, e.g. $76 - 20$ as 76, 66, 56 or in one hop
 $76 - 20 = 56$

Subtract two 2-digit numbers by counting back in tens then in ones, e.g.
 $67 - 33$ as 67 subtract 30 (37) then count back 3 (34)

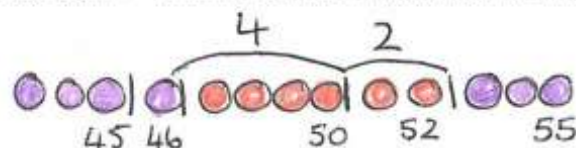
Subtracting near multiples, e.g. $74 - 21$ or $57 - 19$

Using number facts

Know pairs of numbers which make the numbers up to and including 10, e.g. $10 - 6 = 4$, $8 - 3 = 5$, $5 - 2 = 3$, etc.

Patterns of known facts, e.g. $9 - 6 = 3$, so we know $39 - 6 = 33$, $69 - 6 = 63$, $89 - 6 = 83$

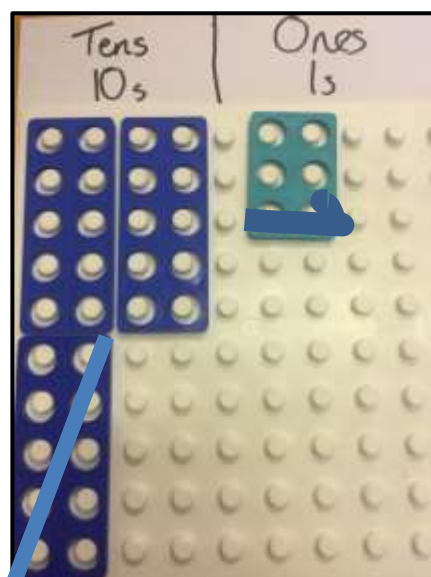
Bridge ten, e.g. $52 - 6$ as 52 subtract 2 then subtract 4 more



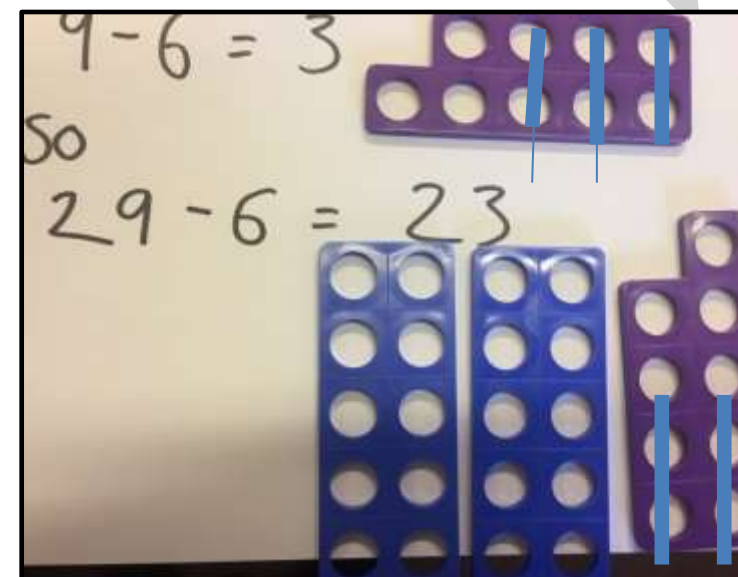
Counting up

Find a difference between two numbers on a line, e.g. $51 - 47$

36 - 12 Using place value



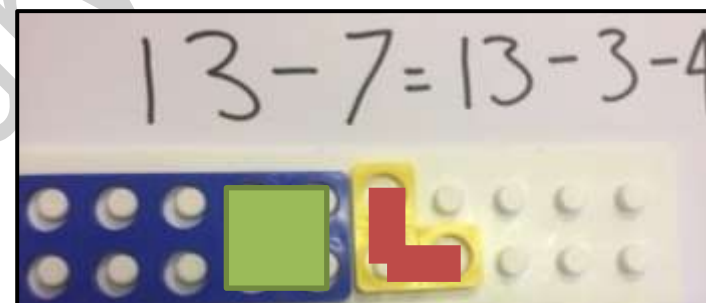
Using number facts



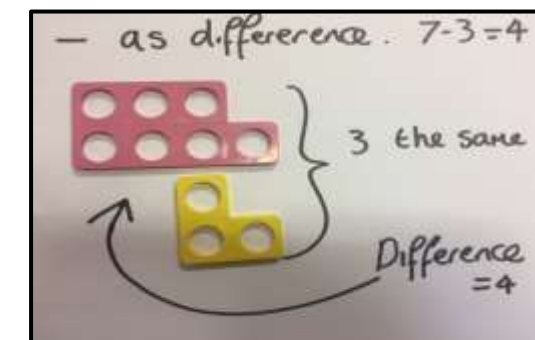
Knowing number facts to 10



Using known facts for bridging ten



Subtraction as difference (counting up)



The bar model can be used to explore the relationship between addition and subtraction.

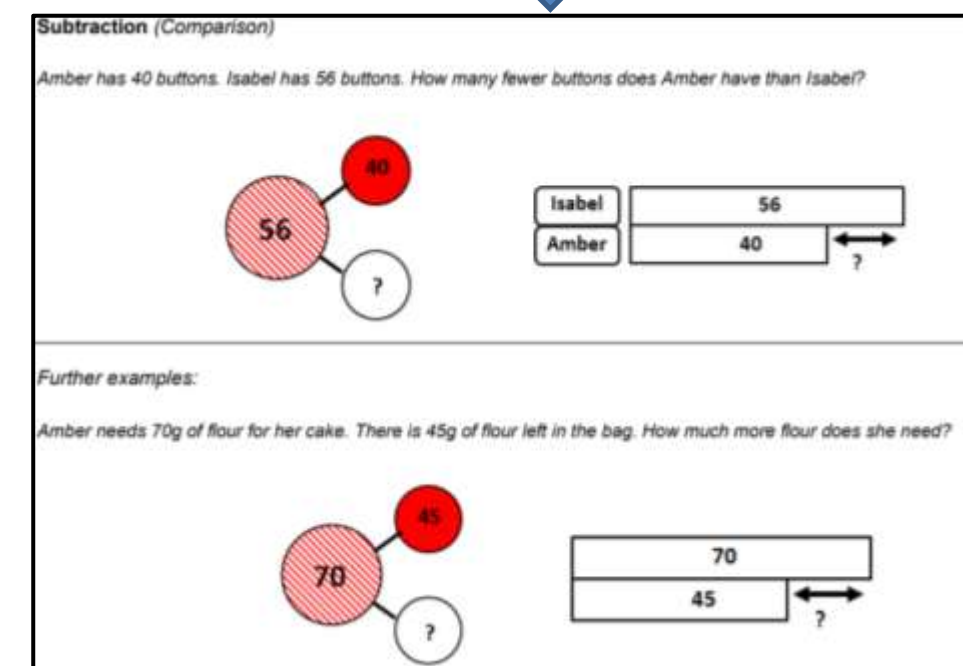
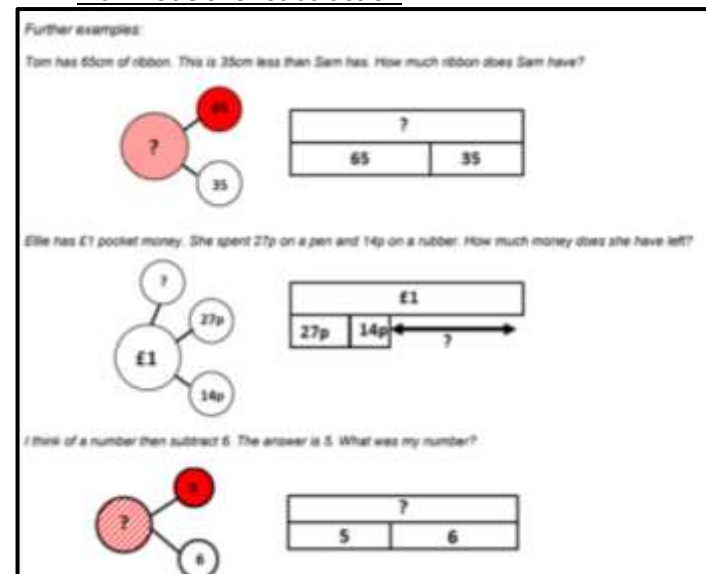
It also shows that addition is commutative (can be done in any order) but subtraction is not.

22	69	47
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$$\begin{array}{l} 69 = 22 + 47 \\ 47 + 22 = 69 \\ 47 = 69 - 22 \\ 69 - 47 = 22 \\ 22 = 69 - \square \end{array}$$



Bar models for subtraction



Year 2 Multiplication

Counting in steps ('Clever' counting)
Count in 2s, 5s and 10s

Begin to count in 3s

Doubling and halving
Begin to know doubles of multiples of 5 to 100, e.g. double 35 is 70

Grouping
Use arrays to find answers to multiplication and relate to 'clever' counting, e.g. 3×4 as three lots of four things and 6×5 as six steps in the 5s count as well as six lots of five

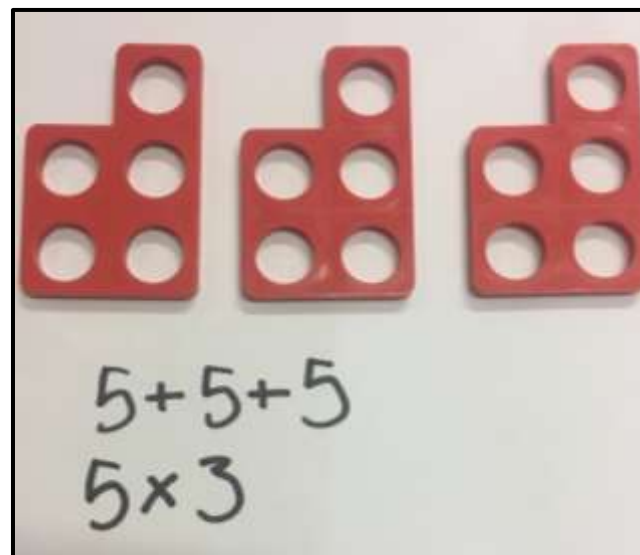
Understand that 5×3 can be worked out as three 5s or five 3s

Using number facts
Know doubles to double 20

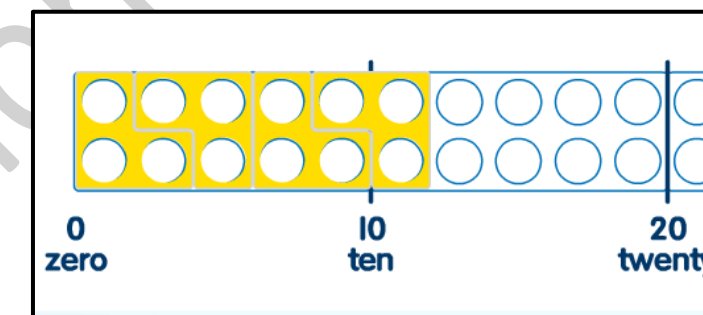
Double 7 = 14

Start learning 2x, 5x, 10x tables, relating these to 'Clever counting' in 2s, 5s, and 10s, e.g. $5 \times 10 = 50$, and 10, 20, 30, 40, 50 is five steps in the tens count

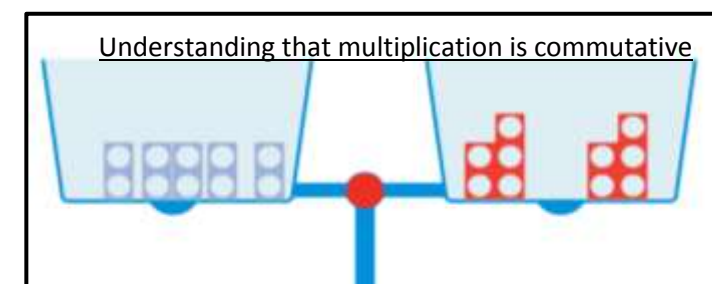
Multiplication as repeated addition



4 groups of 3 using repeated addition and a number line

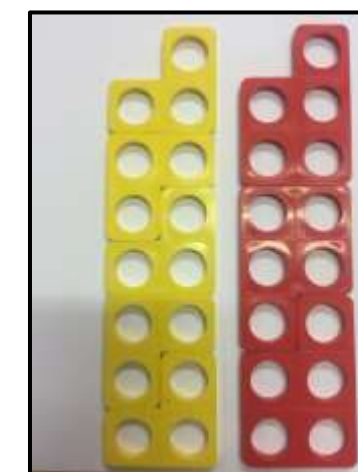
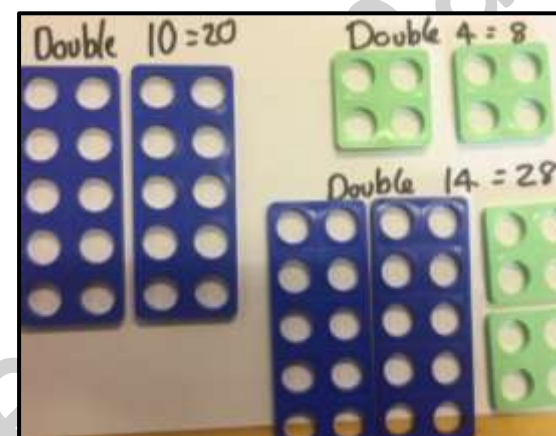


Understanding the commutative law



Understanding the commutative law

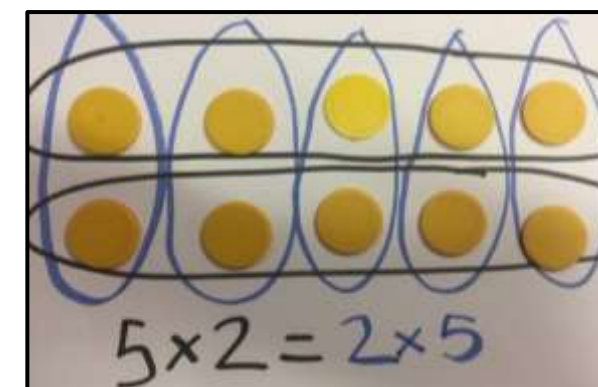
Knowing doubles to double 20



Multiplication - Equal groups
(It is important that children start to understand unitisation at this point)
James buys four tickets for the football match. Each ticket costs £5. How much does he spend?

Four groups of £5 is £20.
£5 four times is £20.

$£5 + £5 + £5 + £5 = £20$
 $4 \times £5 = £20$



Year 2 Division

Counting in steps ('Clever' counting)
Count in 2s, 5s and 10s

Doubling and halving
Find half of numbers up to 40, including realising that half of an odd number gives a remainder of 1 or an answer containing a $\frac{1}{2}$
Begin to know half of multiples of 10 to 100, e.g. half of 70 is 35

Grouping
Relate division to multiplication by using arrays or towers of cubes to find answers to division, e.g. how many towers of five cubes can I make from 20 cubes as $\square \times 5 = 20$ and also as $20 \div 5 = ?$

Relate to division to 'clever' counting and hence to multiplication, e.g. how many 5s do I count to get to 20?

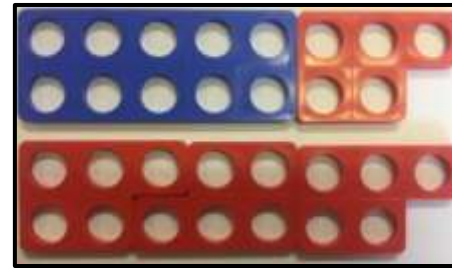
Sharing
Begin to find half or a quarter of a quantity using sharing, e.g. $\frac{1}{4}$ of 16 cubes by sorting the cubes into four piles
Find $\frac{1}{4}$, $\frac{1}{2}$, $\frac{3}{4}$ of small quantities

Children learn that division is not commutative

Using number facts
Know halves of even numbers to 24
Know 2x, 5x and 10x division facts
Begin to know 3x division facts



15 divided by 3 as grouping



18 divided by 5 as grouping showing remainders



Division: Grouping
Claire wants to put 5 biscuits on each plate. She has 20 biscuits. How many plates does she need?

$20 \div 5 = 4$
 $4 \times 5 = 20$

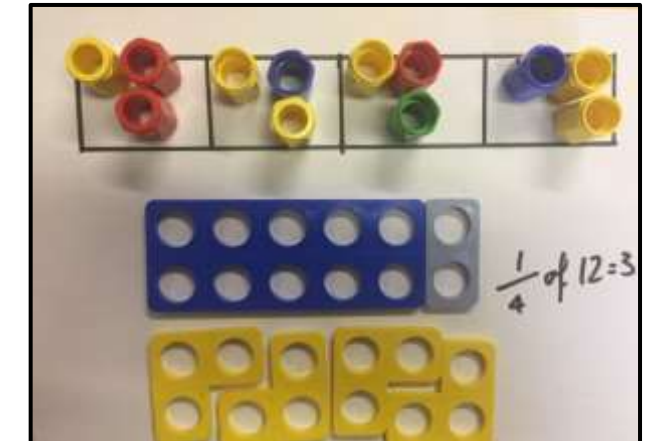
There are 4 groups of 5 in 20.

Division - Sharing
There are 20 children in the hall. The teacher wants to put the children into 4 equal teams. How many children are in each team?

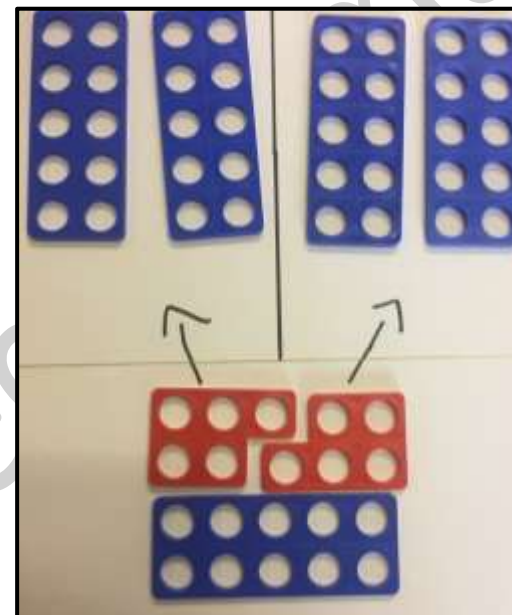
20 shared equally between 4 groups results in 5 in each group.

$20 \div 4 = 5$
 $4 \times 5 = 20$

Division as sharing, linked to fractions



Halving multiples of 10 (50)



The bar model and fractions

Explore the different fractions using Cuisenaire rods and multilinking cubes

Half

What fractions do you see?
If the orange is worth 6, what is the value of the yellow?
If each of the yellow rods is worth 8, what is the value of the orange?
If the orange is worth 100, what is the value of the yellow?

What is half of 20?
 $20 \div 2 = ?$

Half of a number is 7, what is the number?
 $? \div 2 = 7$

Repeat similar questions with the other fractions

Quarters

What is one quarter of 16?
What is $\frac{3}{4}$ of 16?

One quarter of a number is 5, what is the number?
 $? \div 4 = 5$

Thirds

$30 \div 3 = ?$

$? \div 3 = 3$

Year 3 Addition

Use place value and partitioning 46p+55p

Use place value and partitioning 232 + 20

n Fill and bridge ten (revised year

Mental Addition

Using Place value
Count in hundreds, e.g. knowing $475 + 200$ as 475, 575, 675

450 475 550 575 650 675

Add multiples of 10, 100 and £1, e.g. $746 + 200$ or $746 + 40$ or $£6.34 + £5$ as $£6 + £5$ and 34p
Partitioning, e.g. $68 + 74$ as $60 + 70$ and $8 + 4$ and combine the totals: $130 + 12 = 142$ or $£8.50 + £3.70$ as $£8 + £3$ and 50p + 70p and combine: $£11 + £1.20$

Counting on
Add two 2-digit numbers by adding the multiple of ten then the ones, e.g. $67 + 55$ as 67 add 50 (117) add 5 (122)
Add near multiples of 10 and 100, e.g. $67 + 39$ or $364 + 199$
Count on from 3-digit nos, e.g. $247 + 34$ as $247 + 30$ (277) then $277 + 4 = 281$

Using number facts
Number bonds to 100, e.g. $35 + 65$, $46 + 54$, $73 + 27$, etc.
Add to next ten and next hundred, e.g. $176 + 4 = 180$, $435 + 65 = 500$, etc.

Written Addition

Significant time with expanded methods before compact. Methods demonstrate alongside each other

400	60	6
+ 300	50	8
700 110 14		

400	60	6
+ 300	50	8
100	10	
800	20	4

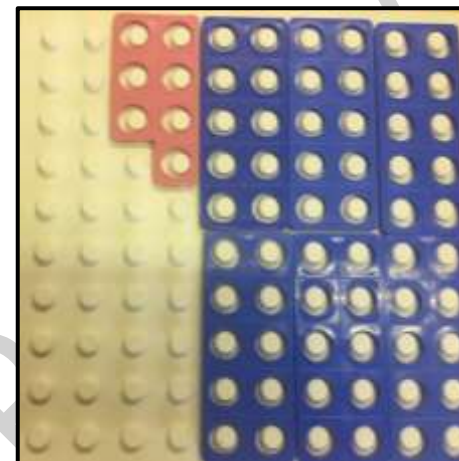
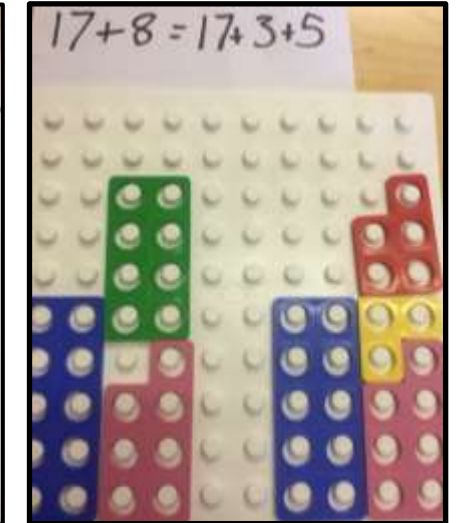
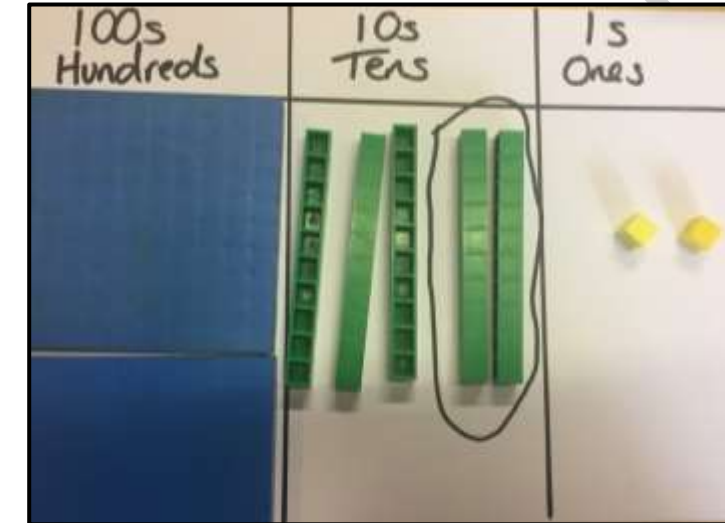
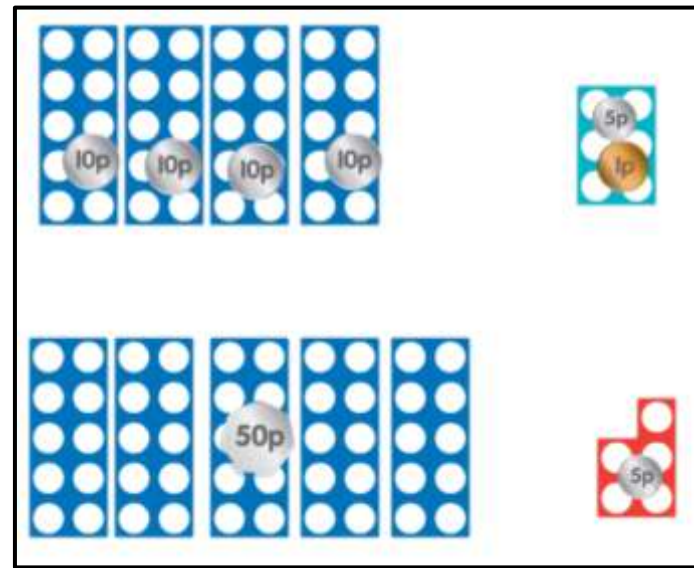
3	4	7
2	8	6
4	9	5
2	1	
1	1	2
1	1	2

Expanded column addition with 'carrying'

Compact column addition with two or more 3-digit numbers or towers of 2-digit numbers

Compact column addition with 3-digit and 4-digit numbers

Recognise fractions which add to 1, e.g. $\frac{1}{4} + \frac{3}{4}$ or $\frac{2}{5} + \frac{3}{5}$



Addition

In a cricket match, James' team score 157 runs in the first innings and 159 in the second innings. How many runs did they score in total?

157	159
?	

James scored 35 more points than Sam. Sam scored 167 points in his game. How many points did James score?

James	?
Sam	167

Know number bonds to 100 (33+67)

Add and adjust $33 + 29 = 33 + 30 - 1$

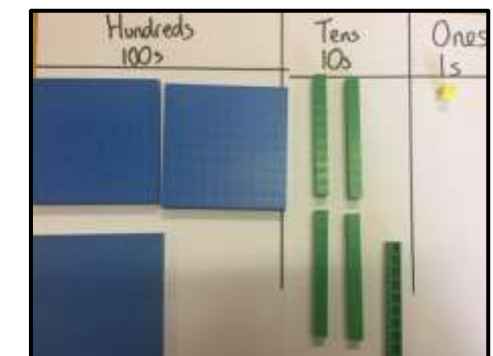
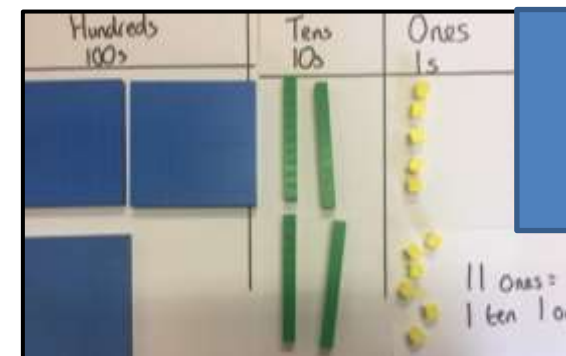
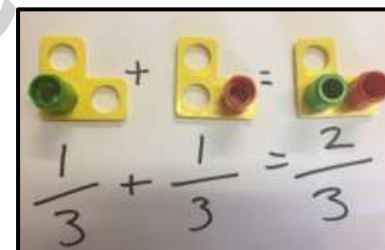
Bar model for addition

Build on partitioning to develop expanded column addition

Add and subtract fractions within the same denominator within one whole

Ensure that the children define the fractions with reference to the whole.

$\frac{5}{7} + \frac{1}{7}$ is equal to $\frac{6}{7}$ of the whole



Adding fractions with the same denominator

Year 3 Subtraction

Using place value to subtract $346 - 40 = 306$

Subtracting by partitioning $38 - 22$ Using known facts for bridging ten(revise)

Mental Subtraction

Taking away
Use place value to subtract, e.g. $348 - 300$ or $348 - 40$ or $348 - 8$
Taking away multiples of 10, 100 and £1, e.g. $476 - 40 = 436$, $476 - 300 = 176$, $£4.76 - £2 = £2.76$
Partitioning, e.g. $68 - 42$ as $60 - 40$ and $8 - 2$ or $£6.84 - £2.40$ as $£6 - £2$ and $80p - 40p$
Count back in hundreds, tens then ones, e.g. $763 - 121$ as $763 - 100$ (663) then subtract 20 (643) then subtract 1 (642)
Subtract near multiples, e.g. $648 - 199$ or $86 - 39$

Counting up
Find a difference between two numbers by counting up from the smaller to the larger, e.g. $121 - 87$

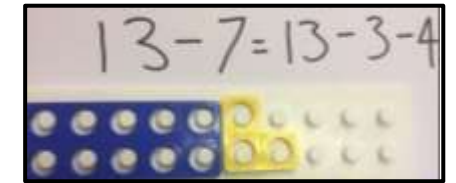
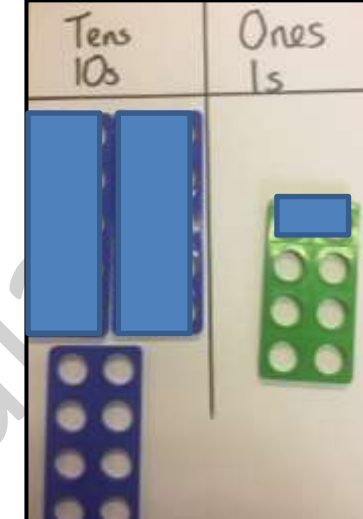
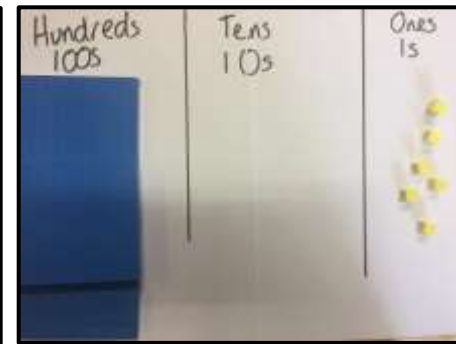
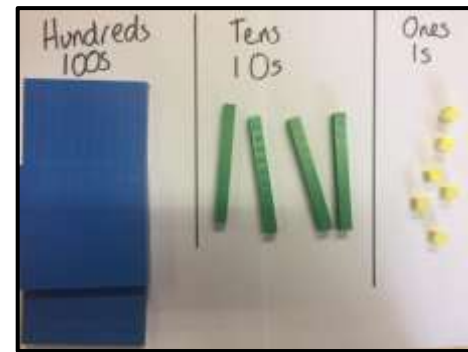
Using number facts
Number bonds to 100, e.g. $100 - 35 = 65$, $100 - 48 = 52$, etc.

Written Subtraction

Develop counting up subtraction

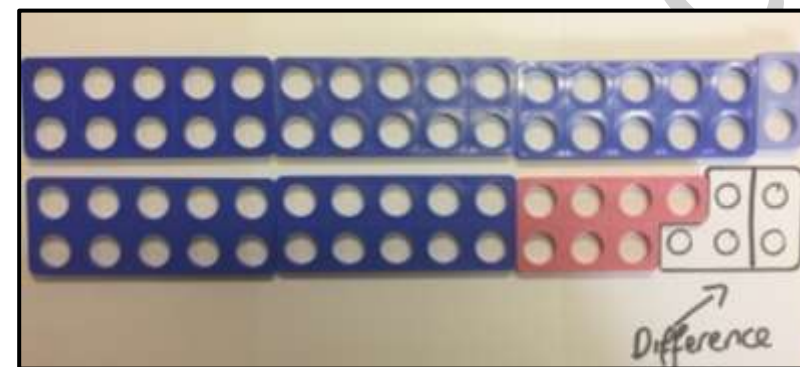
Use counting up subtraction to find change from £1 and £10

Recognise complements of any fraction to 1, e.g. $1 - \frac{1}{4} = \frac{3}{4}$ or $1 - \frac{2}{3} = \frac{1}{3}$



Understanding subtraction as difference by counting up (32-27)

Using the bar model to illustrate the structure of subtraction problems



There are 350 pages in Amber's book. On Tuesday, she reads 167 pages of her book. On Wednesday, she reads the rest of the book. How many pages did she read on Wednesday?

James has collected 23 fewer football stickers than Sam. Sam has collected 97. How many football stickers has James collected?

The bag of flour weighs $\frac{3}{4}$ kg. Nicola uses 600g of flour. How much flour

What story problems could these bar models represent?

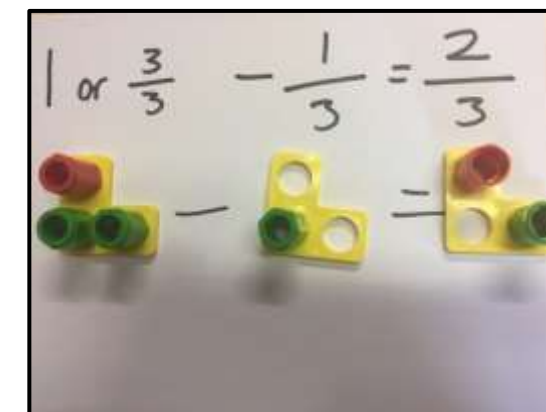
No column subtraction until year 4

Subtraction of fractions with the same denominator

Subtraction

Take away model
 $\frac{3}{5} - \frac{2}{5} = ?$

Comparison model
The difference between $\frac{3}{5}$ and $\frac{2}{5}$ is $\frac{1}{5}$ of the whole



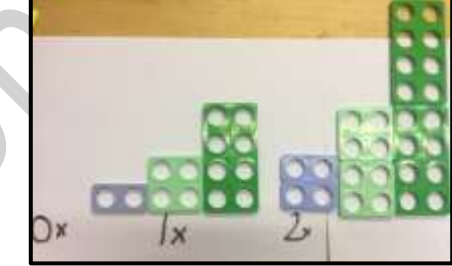
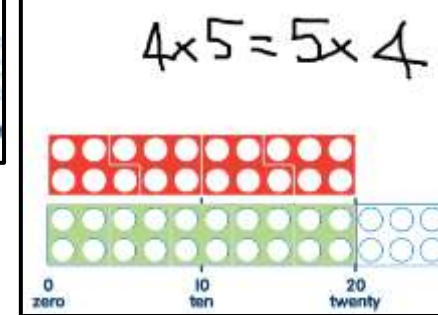
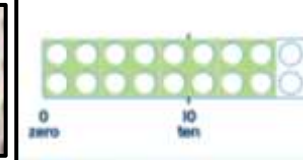
Year 3 Multiplication

Repeated addition

Linked to number line

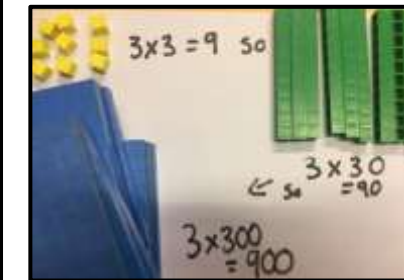
x is commutative (see year)

Recognise link between 2,4,8s and 5 and 10s



Use place to multiply multiples of 10/100

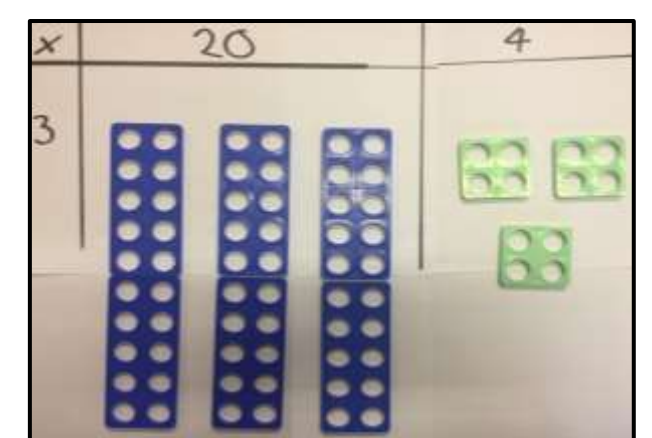
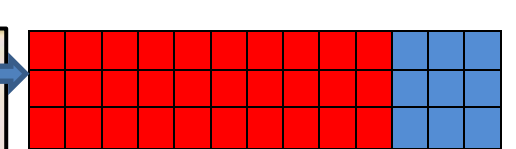
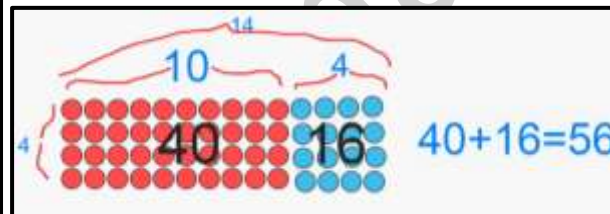
Partitioning to double



Return to arrays

Move on to using groups of 10

Drawing arrays prepares for area in year 4



Mental Multiplication

Counting in steps ('Clever' counting)
Count in 2s, 3s, 4s, 5s, 8s and 10s, e.g. colour the multiples on a 1-100 grid or use hops along a landmarked line

Doubling and halving
Find doubles to double 50 using partitioning
Use doubling as a strategy in multiplying by 2
E.g. 18×2 is double 18 (36)

$40 \times 2 = 80$ $8 \times 2 = 16$ 96

Grouping
Recognise that multiplication is commutative, e.g. $4 \times 8 \equiv 8 \times 4$
Multiply multiples of 10 by single digit numbers, e.g. $30 \times 8 = 240$
Multiply friendly 2-digit numbers by single digit numbers, e.g. 13×4

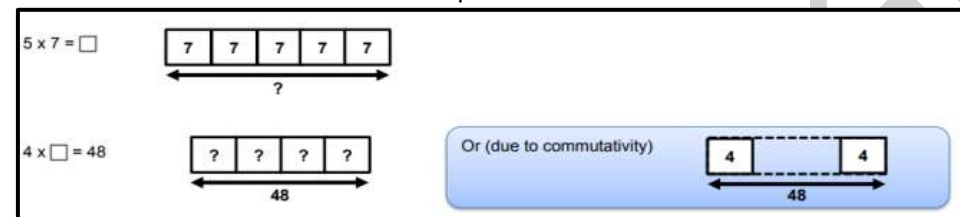
Using number facts
Know doubles to 20 and doubles of multiples of 5 to 100, e.g. double 45 is 90
Know doubles of multiples of 5 to 100, e.g. double 85 is 170
Know 2x, 3x, 4x, 5x, 8x, 10x tables facts

Written Multiplication

Build on partitioning to develop grid multiplication

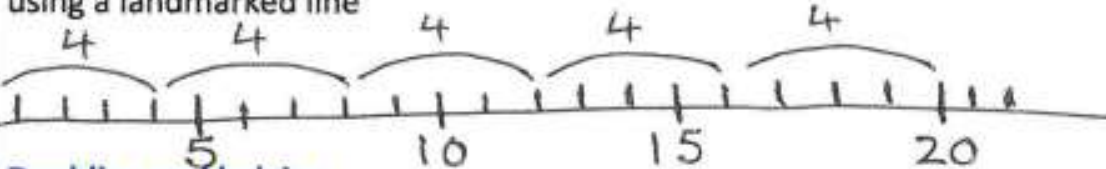
x	20	3	
4	80	12	= 92

Bar models for multiplication

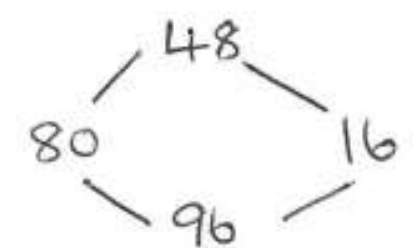


Year 3 Division

Counting in steps ('Clever' counting)
Count in 2s, 3s, 4s, 5s, 8s and 10s by colouring numbers on the 1-100 grid or using a landmarked line



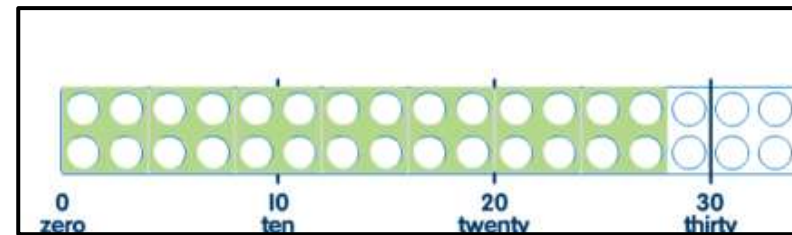
Doubling and halving
Find half of even numbers to 100 using partitioning.
Use halving as a strategy in dividing by 2.
E.g. $36 \div 2$ is half of 36



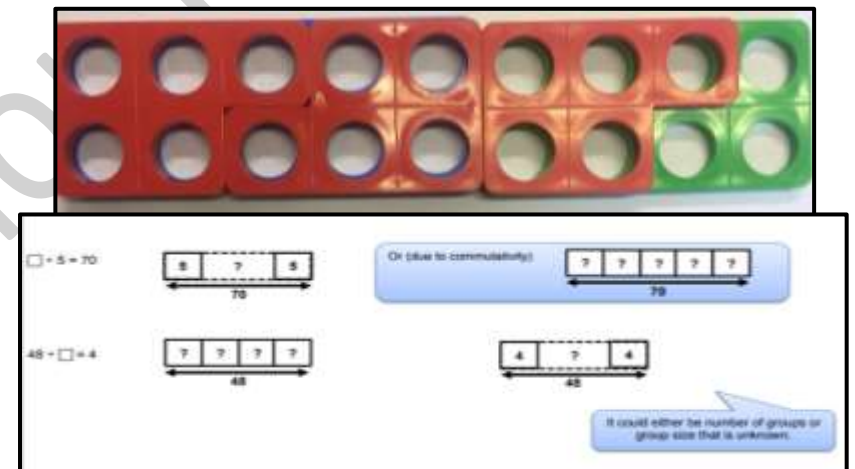
Grouping
Recognise that division is not commutative, e.g. $16 \div 8$ does not equal $8 \div 16$
Relate division to multiplications 'with holes in', e.g. $\square \times 5 = 30$ is the same calculation as $30 \div 5 = ?$ thus we can count in 5s to find the answer
Divide multiples of 10 by single digit numbers, e.g. $240 \div 8 = 30$

Using number facts
Know halves of even numbers to 40
Know halves of multiples of 10 to 200, e.g. half of 170 is 85
Know 2x, 3x, 4x, 5x, 8x, 10x division facts
Use division facts to find unit and simple non-unit fractions of amounts within the times tables, e.g. $\frac{3}{4}$ of 48 is $3 \times (48 \div 4)$

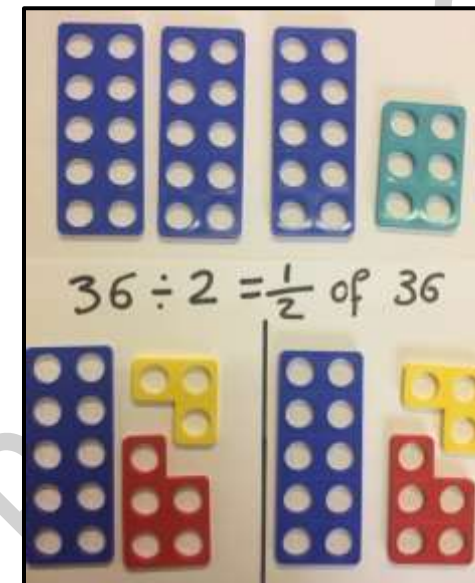
Relative division to multiplication (grouping)



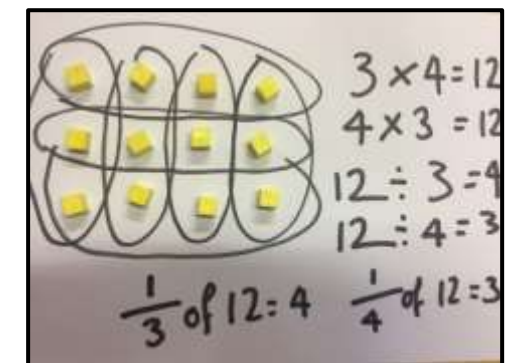
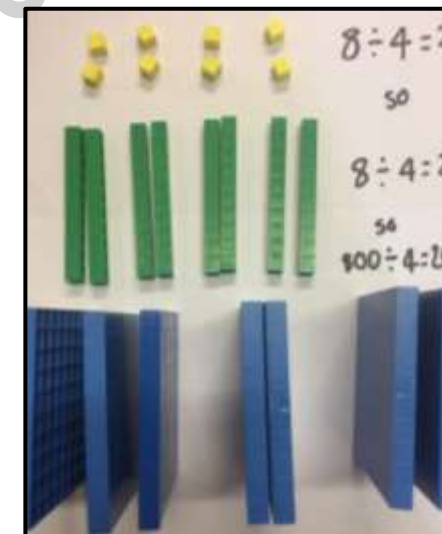
Division as grouping with remainder



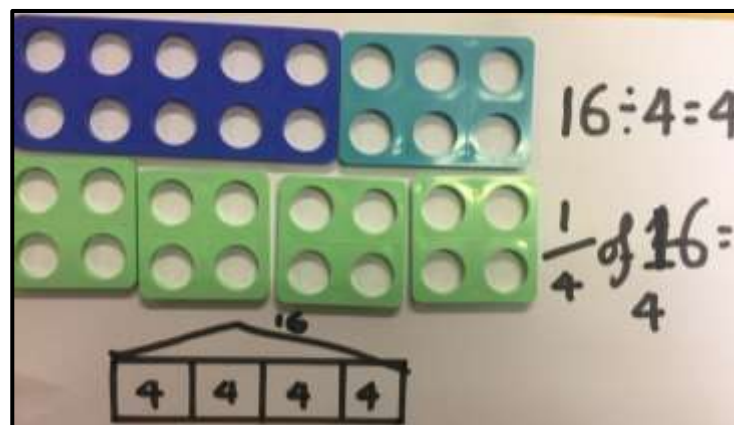
Using partitioning to halve



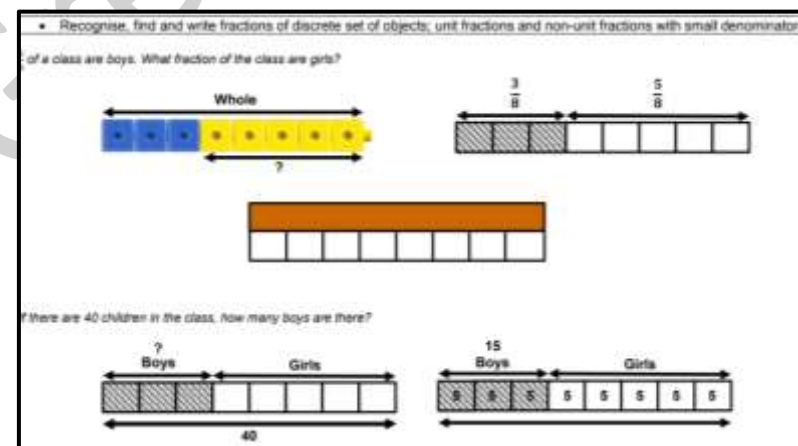
Division with place value sharing numbers greater than 1 Using arrays to link x and division



No formal written division in year 3



Fractions and division



Year 4 Addition

Using Place value

Count in thousands, e.g. knowing $475 + 200$ as 475, 575, 675

Partitioning, e.g. $746 + 203$ as $700 + 200$ and $46 + 3$
or $134 + 707$ as $130 + 700$ and $4 + 7$

Counting on

Add two 2-digit numbers by adding the multiple of ten then the ones, e.g. $67 + 55$ as 67 add 50 (117) add 5 (122)

Add near multiples of 10, 100 and 1000, e.g. $467 + 199$ or $3462 + 2999$



Count on to add 3-digit numbers and money, e.g. $463 + 124$ as $463 + 100$ (563) $+20$ (583) $+4$ =587 or $£4.67 + £5.30$ as $£9.67$ add 30p

Using number facts

Number bonds to 100 and to next multiple of 100, e.g. $463 + 37$, $1353 + 47$



Number bonds to £1 and to the next whole pound, e.g. $£3.45 + 55p$

Add to next whole number, e.g. $4.6 + 0.4$, $7.2 + 0.8$

Build on expanded column addition to develop compact column addition with larger numbers.

1000	400	60	6
+ 4000	800	60	8
1000	100		
6000	300		

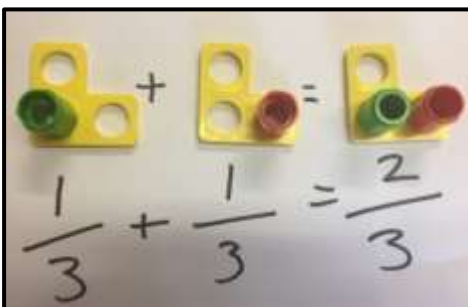
Significant time of expanded methods to consolidate place value. Methods demonstrated side by side

Compact column addition with larger numbers.

5347
2286
+1495
121
9128

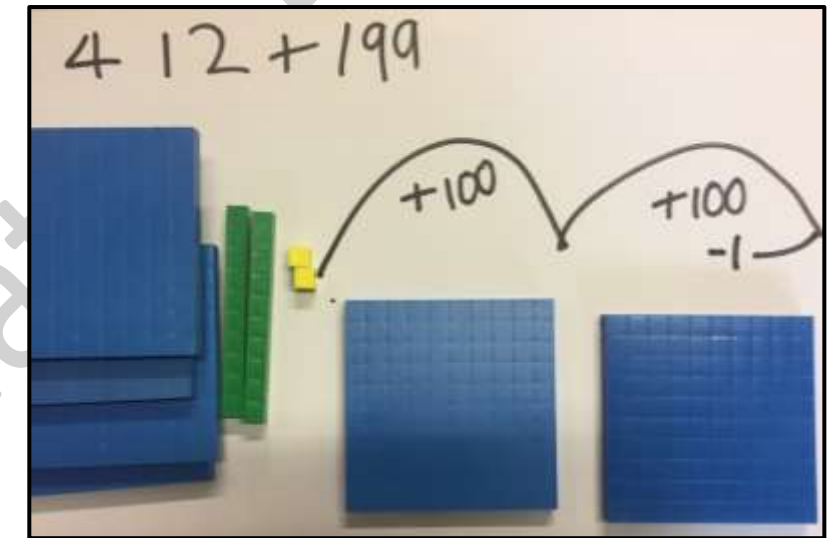
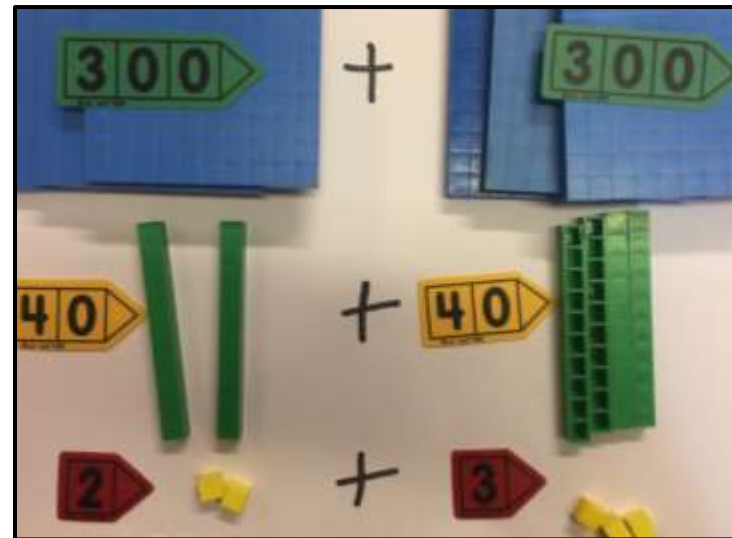
Use expanded and compact column addition to add amounts of money.

Add like fractions, e.g. $\frac{1}{3} + \frac{1}{3} + \frac{1}{3}$

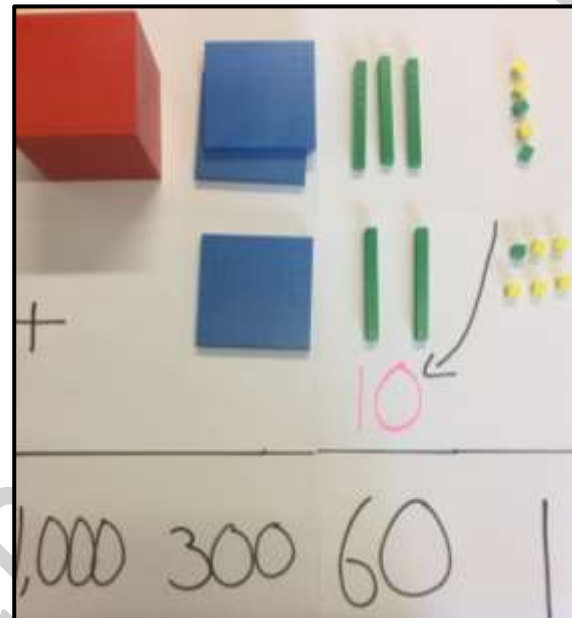


See year 3 bar model for adding fractions

Adding multiples of 10 or 100 and adjusting



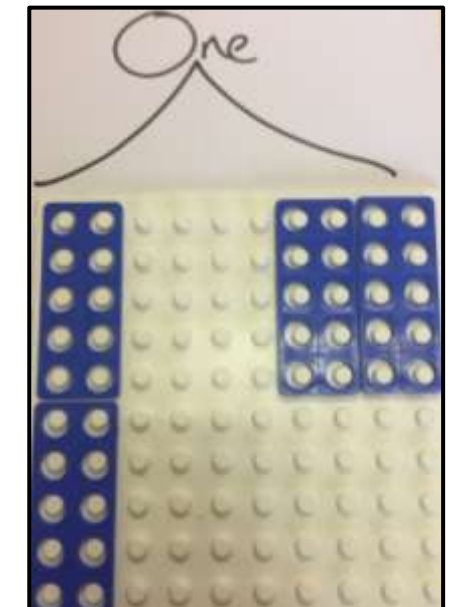
Modelling addition by partitioning



Adding by bridging



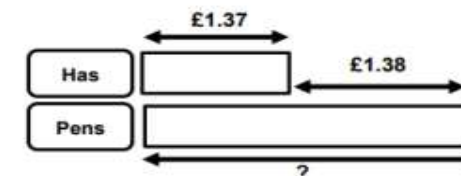
Adding decimals using straws/numicon



Emily is making a cake. She puts flour on the scales. How much sugar does she add?



Claire has £1.37. She needs £1.38 more to buy a packet of pens. How much do the pens cost?



Year 4 Subtraction

Taking away

Use place value to subtract, e.g. $4748 - 4000$ or $4748 - 8$, etc.
Take away multiples of 10, 100, 1000, £1, 10p or 0.1, e.g. $8392 - 50$ or $6723 - 3000$ or $£3.74 - 30p$ or $5.6 - 0.2$
Partitioning, e.g. $£5.87 - £3.04$ as $£5 - £3$ and $7p - 4p$ or $7493 - 2020$ as $7000 - 2000$ and $90 - 20$
Count back, e.g. $6482 - 1301$ as $6482 - 1000$ then $- 300$ then $- 1$ (5181)
Subtract near multiples, e.g. $3522 - 1999$ or $£34.86 - £19.99$

Counting up

Find a difference between two numbers by counting up from the smaller to the larger, e.g. $506 - 387$



Using number facts

Number bonds to 10, 100 and derived facts, e.g. $100 - 76 = 24$, $1.0 - 0.6 = 0.4$
Number bonds to £1 and £10, e.g. $£1.00 - 86p = 14p$ or $£10 - £3.40 = £6.60$

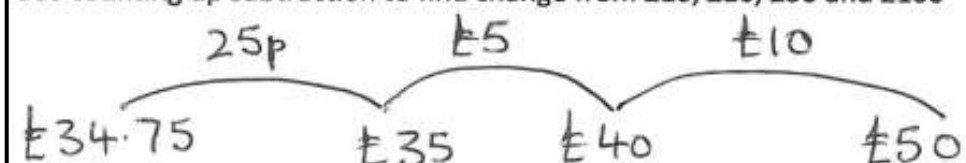
Expanded column subtraction

$$\begin{array}{r} 600 \\ 700 \\ - 300 \\ \hline 300 \end{array} \quad \begin{array}{r} 110 \\ 20 \\ - 50 \\ \hline 60 \end{array} \quad \begin{array}{r} 16 \\ 8 \\ - 8 \\ \hline 8 \end{array}$$

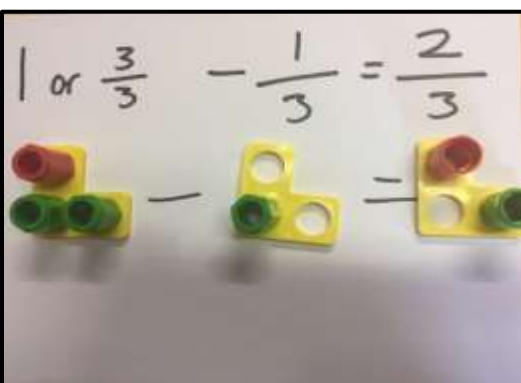
Begin to use compact column subtraction

$$\begin{array}{r} 6116 \\ 728 \\ - 358 \\ \hline 368 \end{array}$$

Use counting up subtraction to find change from £10, £20, £50 and £100

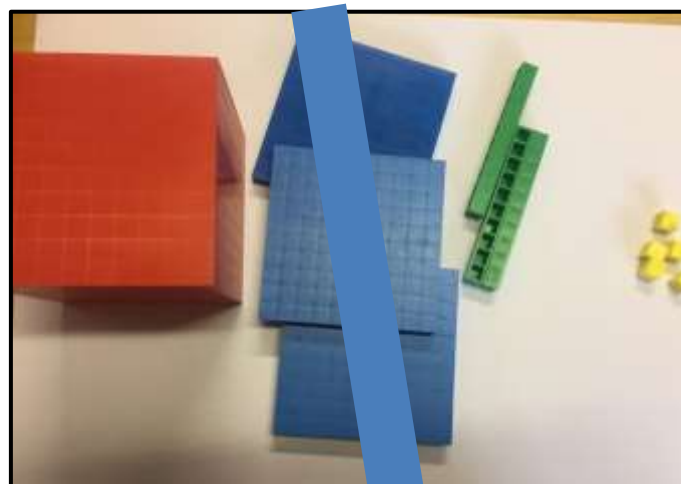


Subtract like fractions, e.g. $\frac{3}{8} - \frac{1}{8} = \frac{2}{8}$

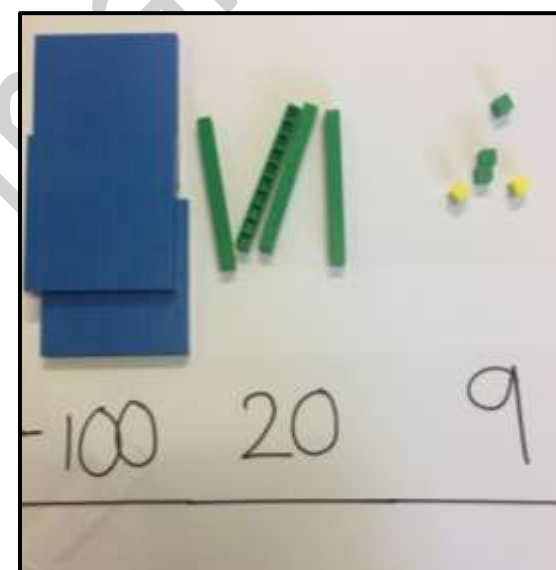
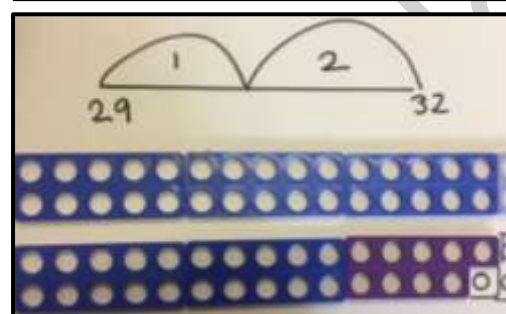


See year 3 bar model for subtracting fractions

Using place value to subtract

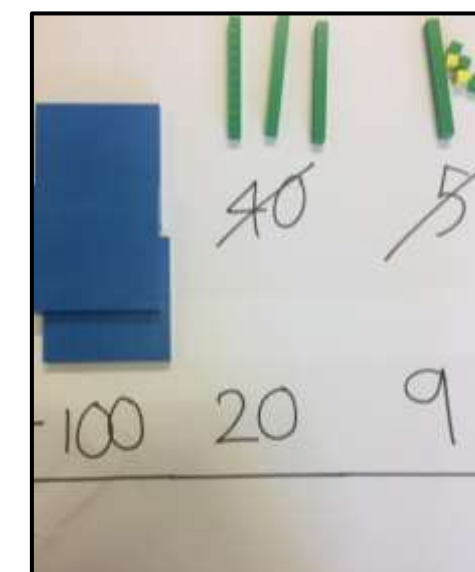
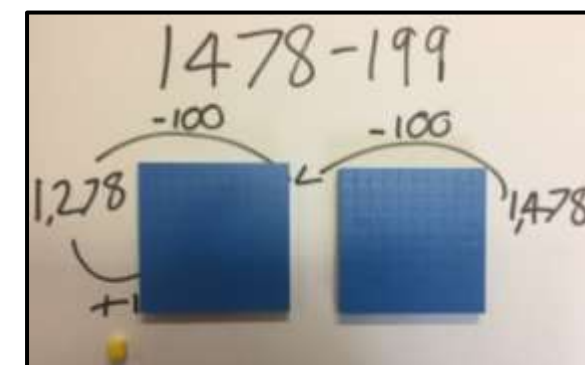
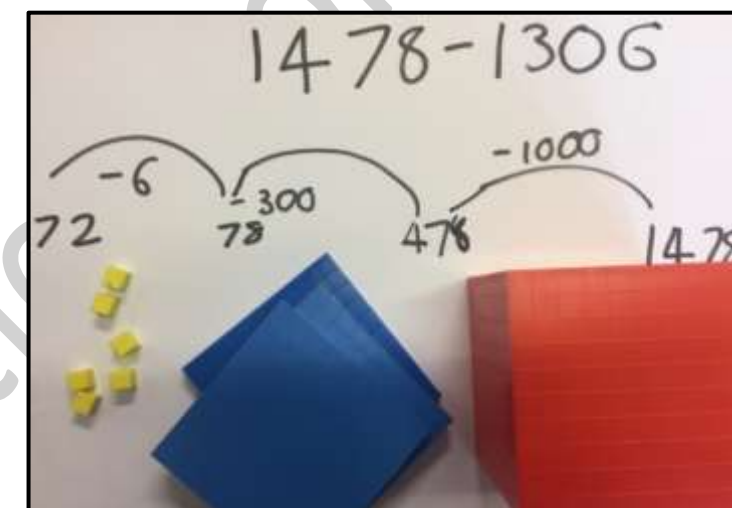


Counting up to find the difference



Modelling subtraction algorithm with dienes blocks

Counting up to the find difference



Year 4 Multiplication

Linked x2 x4 and x8 to doubling Revise partition for doubling and halving as year 3 Bar model for multiplication

Counting in steps – sequences
Count in 2s, 3s, 4s, 5s, 6s, 7s, 8s, 9s, 10s, 11s, 12s, 25s, 50s, 100s and 1000s

Doubling and halving
Find doubles to double 100 and beyond using partitioning
Begin to double amounts of money.
E.g. £3.50 doubled is £7
Use doubling as a strategy in multiplying by 2, 4 and 8, e.g. $34 \times 4 = \text{double } 34 (68) \text{ doubled again } (136)$

Grouping
Use partitioning to multiply 2-digit numbers by single-digit numbers
Multiply multiples of 100 by single digit numbers using tables facts, e.g. $400 \times 8 = 3200$
Multiply using near multiples by rounding, e.g. 24×19 as $(24 \times 20) - 24$

Using number facts - Know times tables up to 12×12

Use grid multiplication to multiply 3-digit by 1-digit numbers

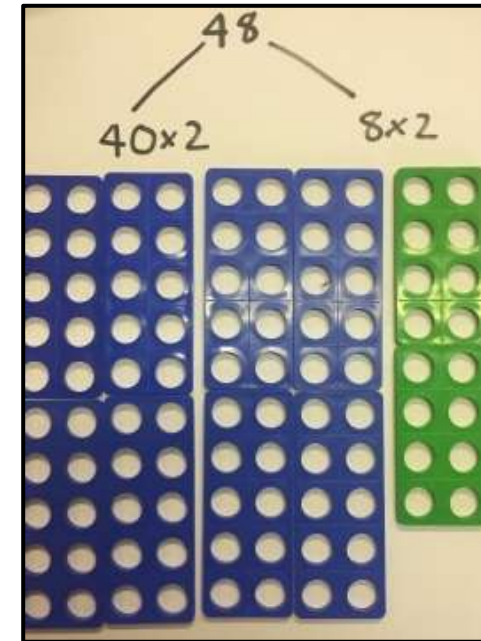
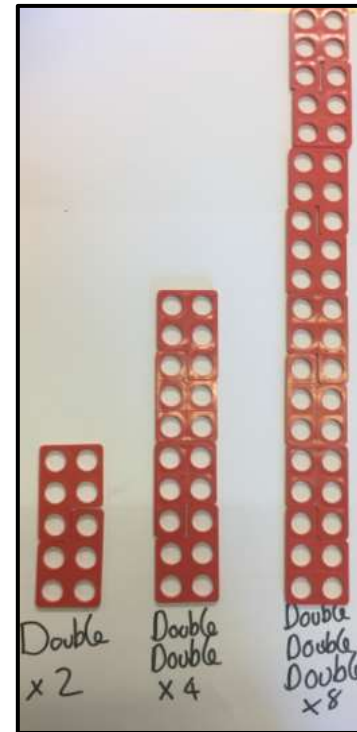
x	200	50	3	
6	1200	300	18	= 1518

Use a vertical written algorithm (ladder) to multiply 3-digit numbers by 1-digit numbers

253
x 6
1518

Use grid multiplication to multiply 2-digit numbers by 2-digit numbers

x	40	6
10	400	60
8	320	48
	720	108
		= 828

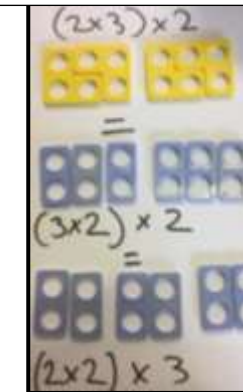


5×0

0 0 0 0 0

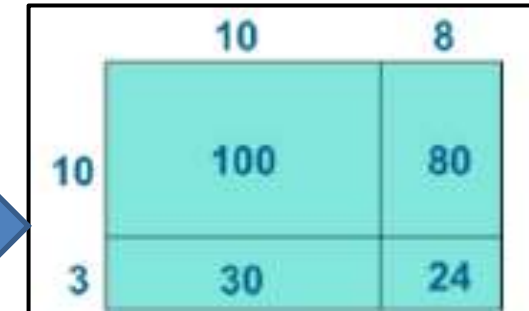
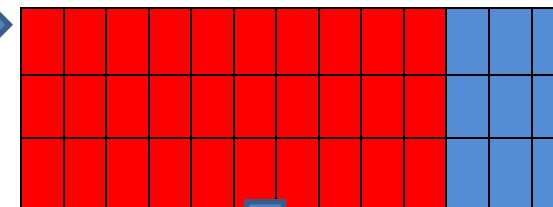
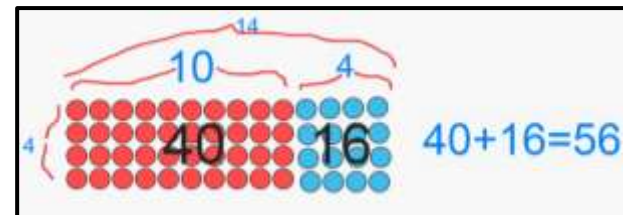
What does this mean?
Use a speaking frame to help support pupils to develop the range of appropriate language.
Number of groups x size of group = total number of objects.
Explore concrete ideas such as 5 plates with no biscuits.
How many biscuits?

Use associative law to x 3 numbers

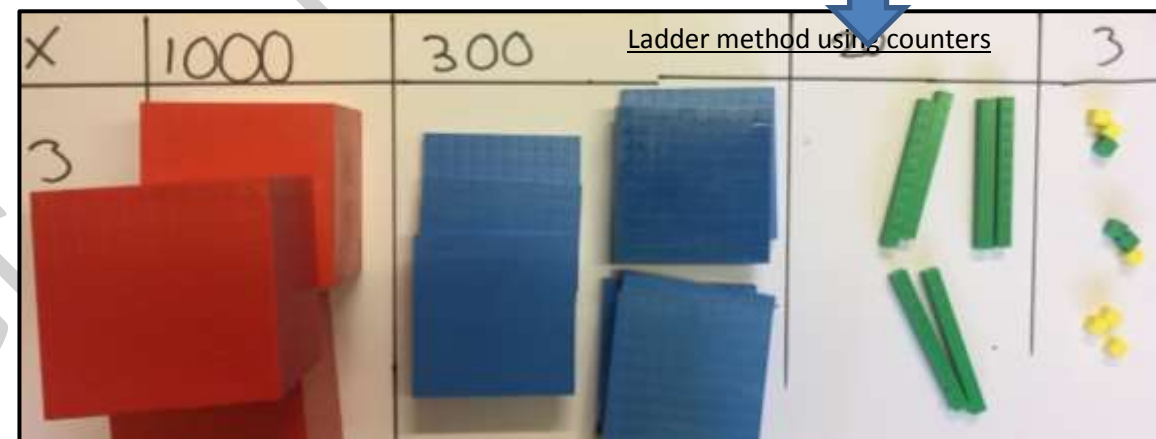
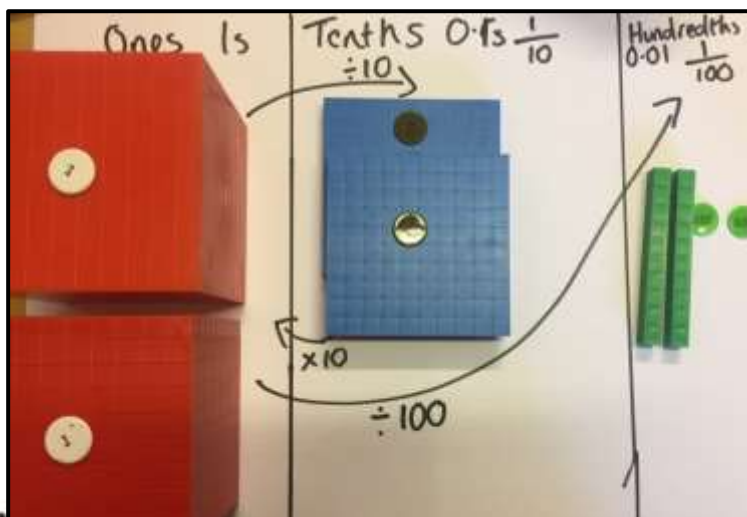


Revise arrays from year 3 (Use Number Gym)

Link knowledge of arrays to area/grid method



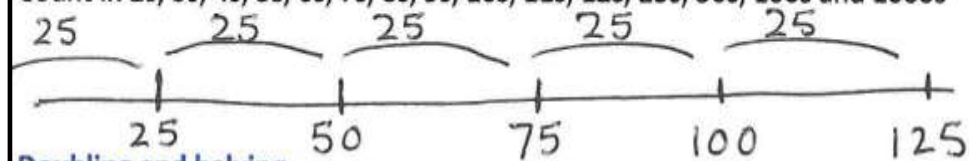
Division/multiplication by 10/100



Year 4 Division

Counting in steps – sequences

Count in 2s, 3s, 4s, 5s, 6s, 7s, 8s, 9s, 10s, 11s, 12s, 25s, 50s, 100s and 1000s



Doubling and halving

Find halves of even numbers to 200

and beyond using partitioning.

Begin to half amounts of money.

E.g. £9 halved is £4.50

Use halving as a strategy in dividing by 2, 4 and 8, e.g. $164 \div 4$ is half of 164

(82) halved again (41)

Grouping

Use multiples of 10 times the divisor to divide

by number ≤ 9 above the tables facts, e.g. $45 \div 3$

Divide multiples of 100 by single digit numbers

using division facts, e.g. $3200 \div 8 = 400$

$$45 \div 3 = \square$$

$$\square \times 3 = 45$$

$$10 \times 3 = 30$$

$$15$$

$$5 \times 3 = 15$$

Using number facts

Know times tables up to 12×12 and all related division facts

Use division facts to find unit and non-unit fractions of amounts within the times tables, e.g. $\frac{7}{8}$ of 56 is $7 \times (56 \div 8)$

Written version of a mental method

$$\square \times 3 = 86 \quad 84 \div 3 = 28 \text{ r}2$$

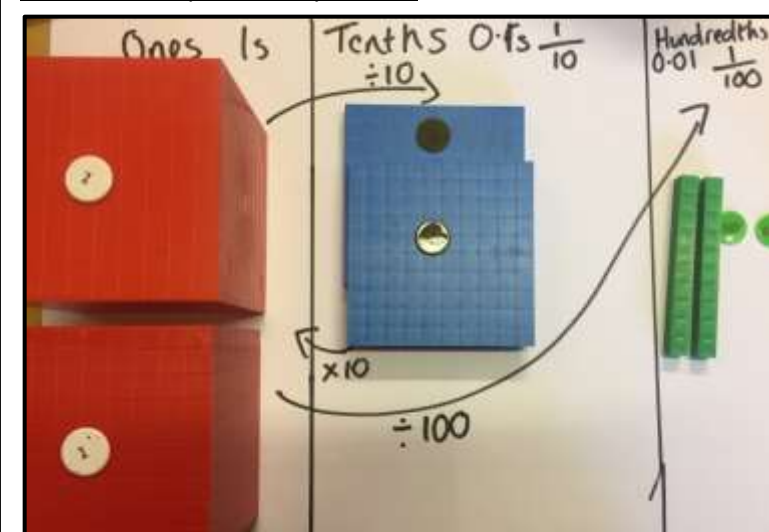
$$20 \times 3 = 60$$

$$26$$

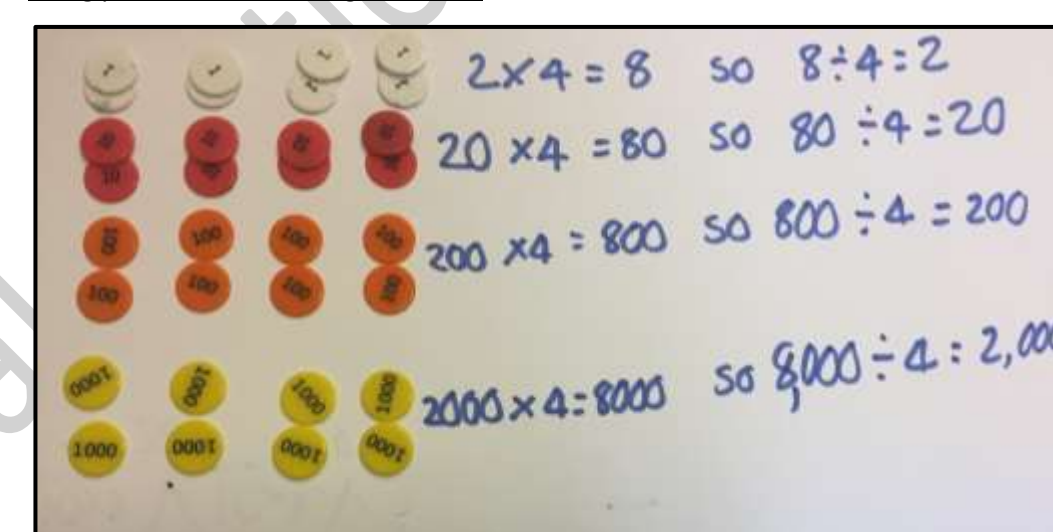
$$8 \times 3 = 24$$

$$2$$

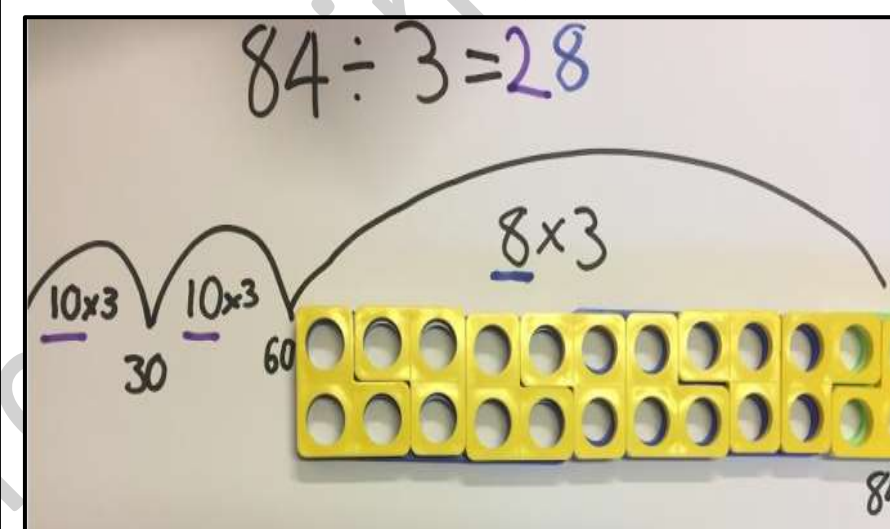
Division/multiplication by 10/100



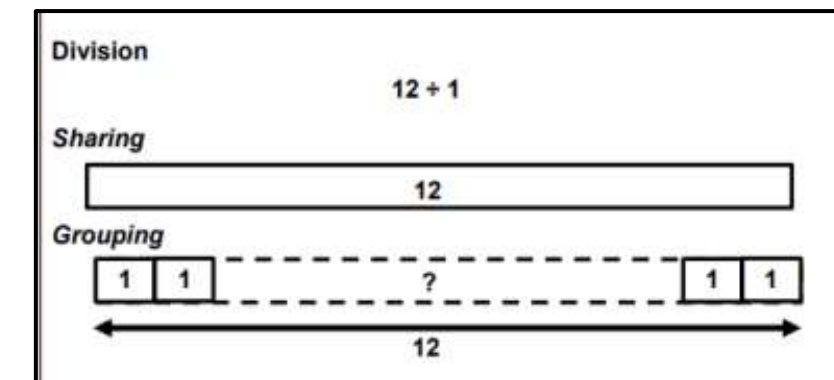
Using place value knowledge to divide



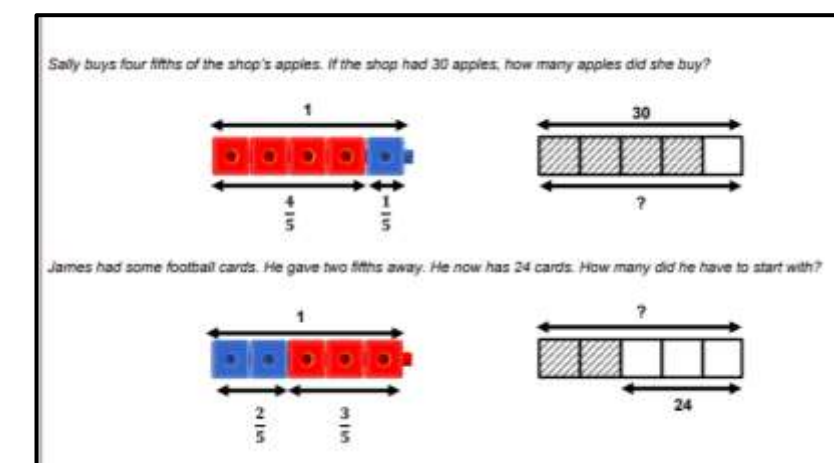
Grouping and using multiples of ten of the divisor



Bar model to show sharing and grouping (sharing leads to fractions)



Bar model for find fractions of a number



Year 5 Mental Addition

Add 0.01 to 1.331

Using Place value
Count in 0.1s, 0.01s, e.g. knowing what 0.1 more than 0.51 is

100s	10s	1s	0.1s	0.01s	0.001s
			5	1	
			6		1

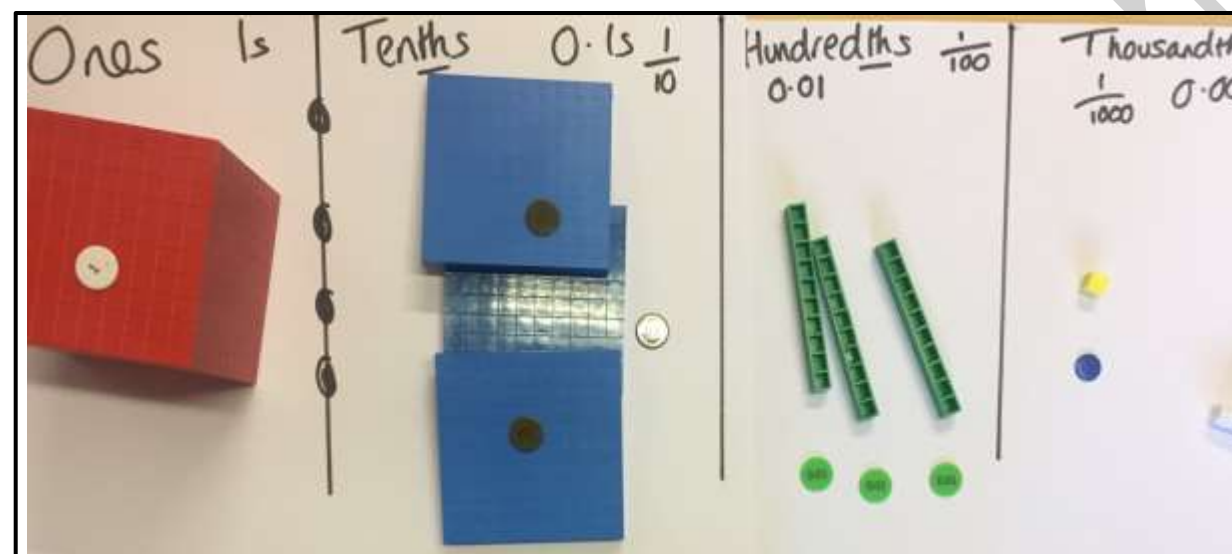
Partitioning, e.g. $2.4 + 5.8$ as $2 + 5$ and $0.4 + 0.8$ and combine the totals: $7 + 1.2 = 8.2$

$$\begin{array}{r} 2.4 \\ + 5.8 \\ \hline 7 + 1.2 = 8.2 \end{array}$$

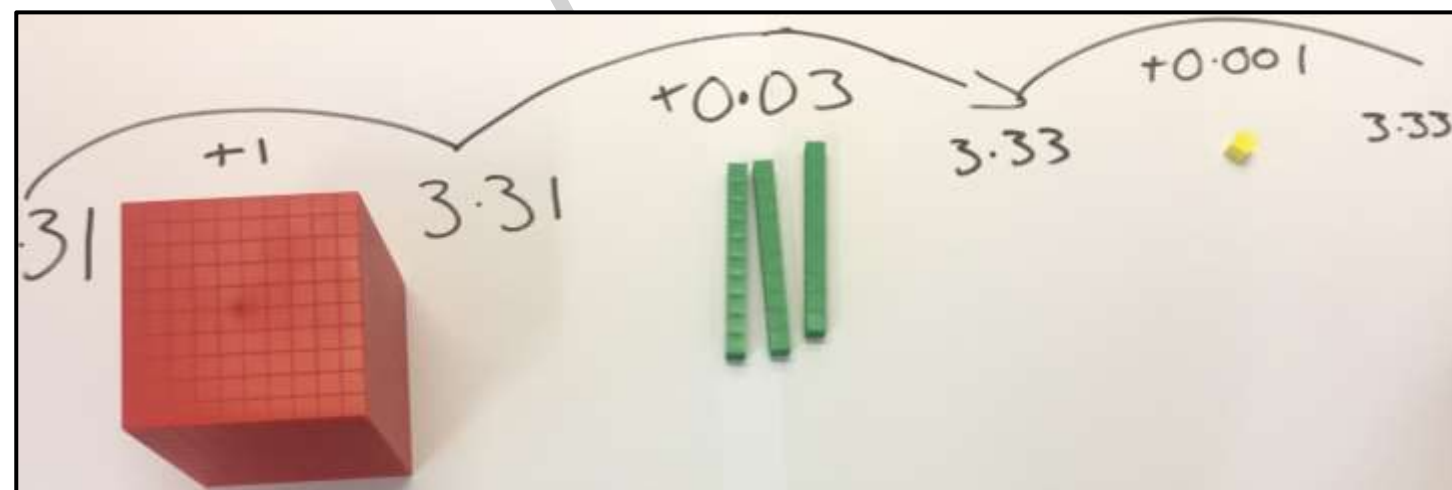
Counting on
Add two decimal numbers by adding the ones then the tenths/hundredths, e.g. $5.72 + 3.05$ as 5.72 add 3 (8.72) then add 0.05 (8.77)
Add near multiples of 1, e.g. $6.34 + 0.99$ or $5.63 + 0.9$
Count on from large numbers, e.g. $6834 + 3005$ as $9834 + 5$

Using number facts
Number bonds to 1 and to the next whole number, e.g. $0.4 + 0.6$ or $5.7 + 0.3$

Add to next ten from a decimal number, e.g. $7.8 + 2.2 = 10$



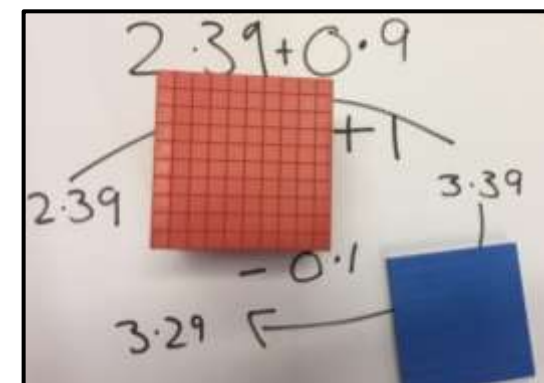
Adding by counting on



Revising understanding of addition from year 4 with year 5

place value expectations

Adding and adjusting $2.39 + 1 - 0.1 = 2.39 + 0.9$



Year 5 Written Addition

Expanded column addition for money leading to compact column addition for adding several amounts of money

$$\begin{array}{r} \text{£}14 \quad 60\text{p} \quad 4\text{p} \\ \text{£}28 \quad 70\text{p} \quad 8\text{p} \\ + \text{£}12 \quad 20\text{p} \quad 6\text{p} \\ \hline \text{£}1 \quad 10\text{p} \\ \text{£}55 \quad 60\text{p} \quad 8\text{p} \end{array}$$

Compact column addition to add Pairs of 5-digit numbers

Continue to use column addition to add towers of several larger numbers.

Use compact addition to add decimal numbers with up to two places

$$\begin{array}{r} 15.68 \\ + 27.86 \\ \hline 11.1 \\ \hline 43.54 \end{array}$$

Adding fractions with same denominators

$$\frac{2}{3} + \frac{2}{3} = \frac{4}{3} \text{ or } 1\frac{1}{3}$$

Using the bar model for ordering and adding fractions with different denominators

$$\frac{1}{3} + \frac{2}{6}$$

• We cannot add fractions with different denominators so....

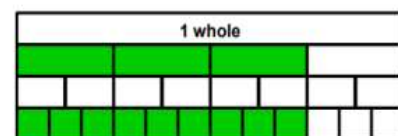
$$\frac{2}{6} + \frac{2}{6}$$

Adding fractions with different denominators

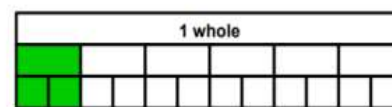
The aim is for the children to discover the relationship and the rule for themselves (see Year 4).

Which fraction is greater $\frac{3}{4}$ or $\frac{1}{6}$?

Three quarters converted into twelfths



One sixth converted into twelfths

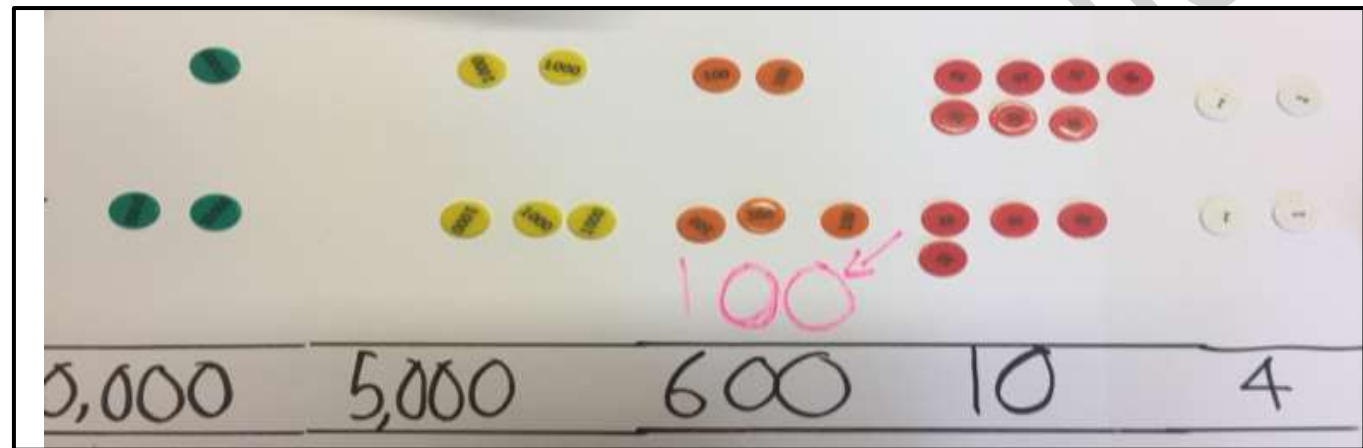


You can compare fractions that have the same numerator by comparing their denominators.

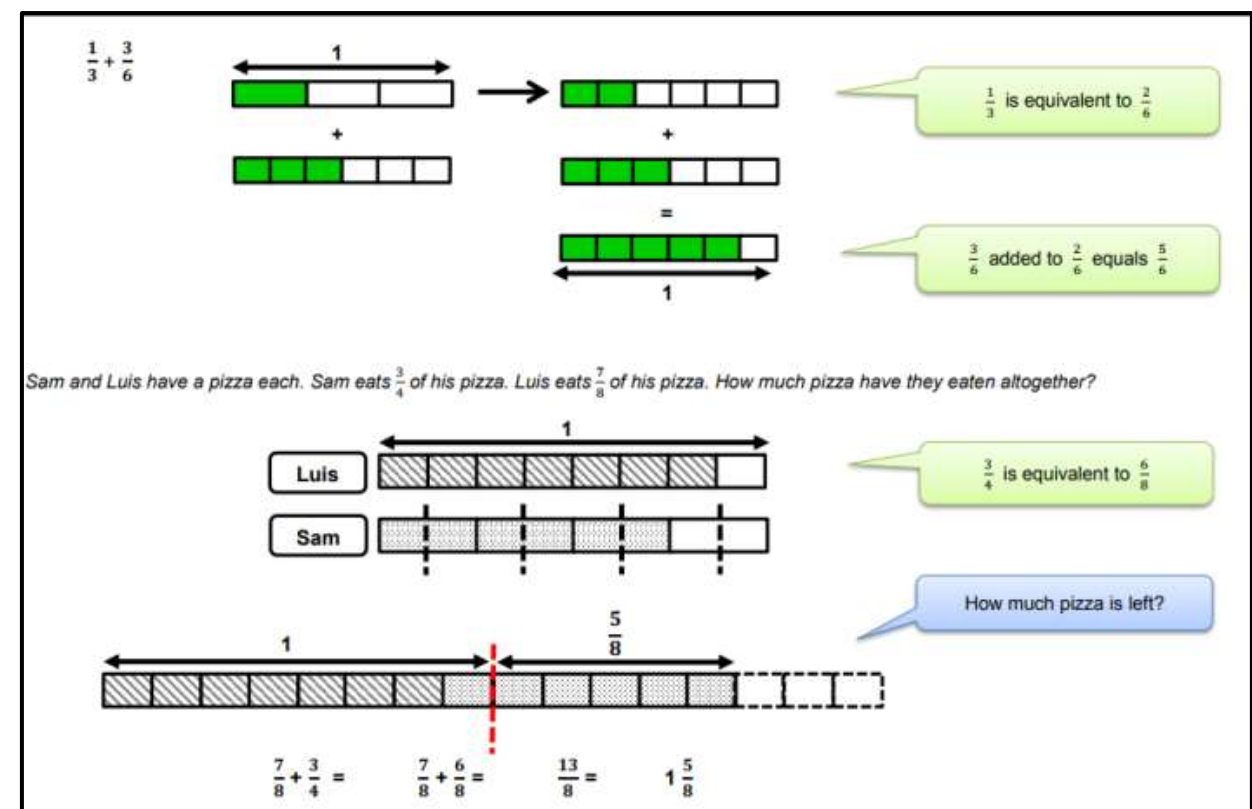
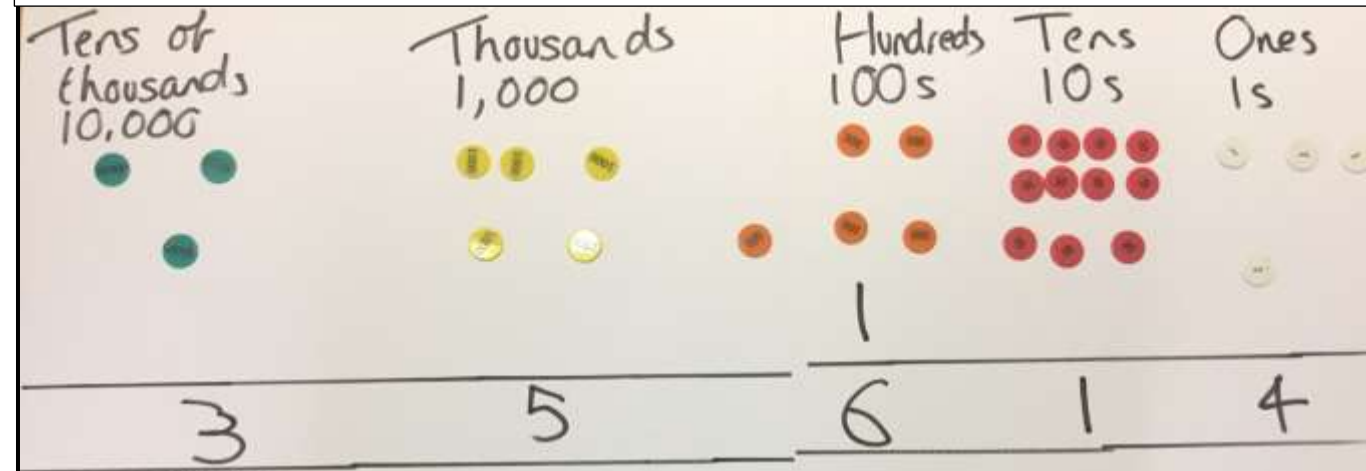
- Which is bigger $\frac{1}{5}$ or $\frac{1}{6}$?

You can compare fractions that have the same denominator by comparing their numerators.

- Which is smaller $\frac{2}{10}$ or $\frac{4}{10}$? How much smaller?



Expanded models consolidate place value up to 1 million in year 5. Similar models to be used with dienes blocks. The same model can be used to investigate addition of decimals



Year 5 Mental Subtraction

Using place value to subtract decimals

Using counters/coins to count up/find the difference

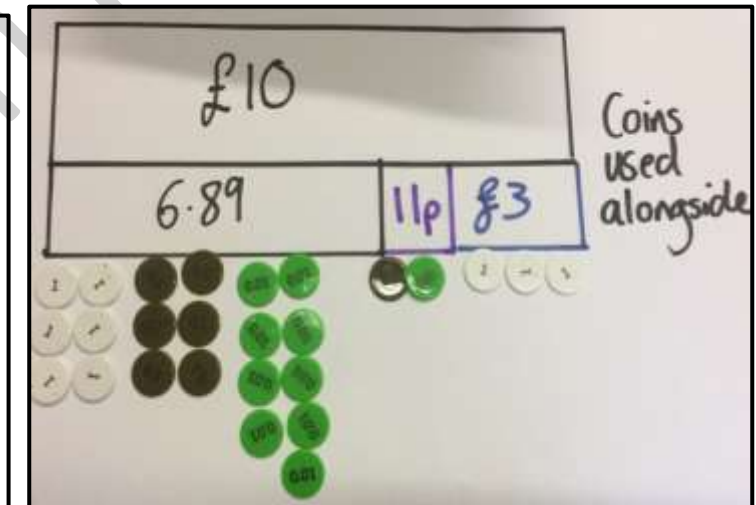
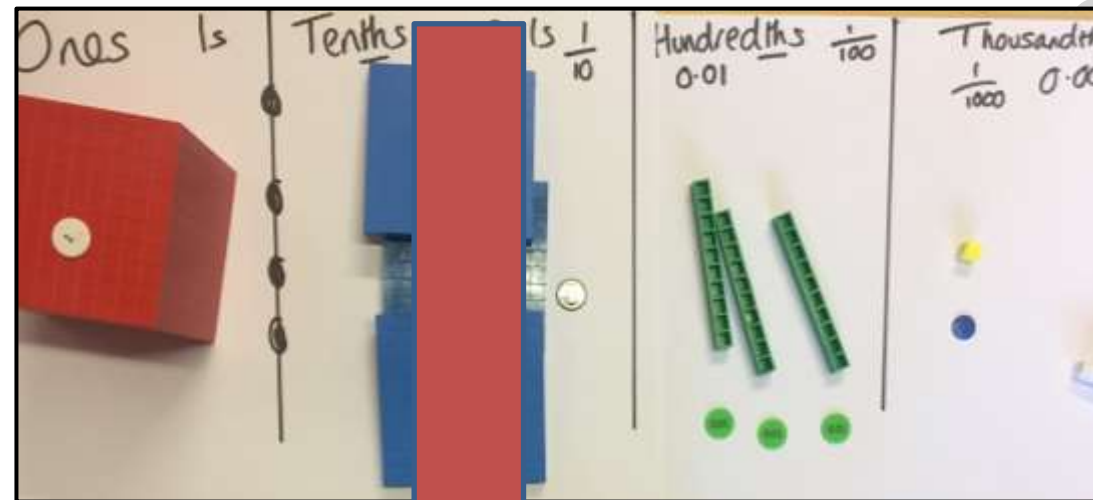
Taking away
Use place value to subtract decimals, e.g. $4.58 - 0.08$ or $6.26 - 0.2$, etc.
Take away multiples of powers of 10, e.g. $15,672 - 300$ or $4.82 - 2$ or $2.71 - 0.5$ or $4.68 - 0.02$
Partition or count back, e.g. $3964 - 1051$ or $5.72 - 2.01$
Subtract near multiples, e.g. $86,456 - 9999$ or $3.58 - 1.99$

Counting up
Find a difference between two numbers by counting up from the smaller to the larger, e.g. $2009 - 869$

Find change using shopkeepers' addition, e.g. buy toy for £6.89 using £10

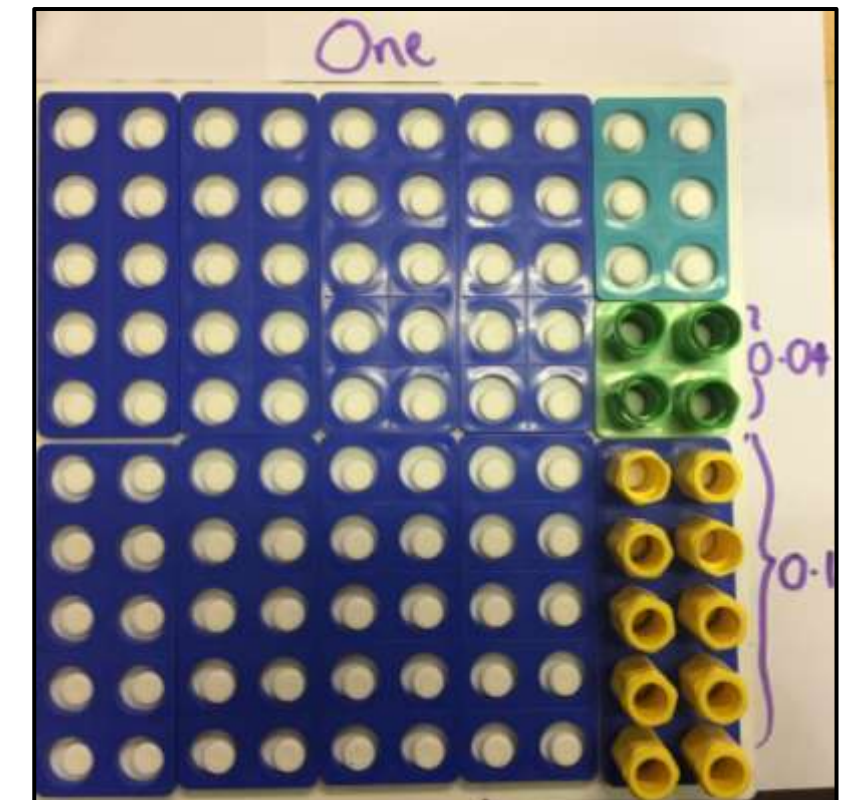
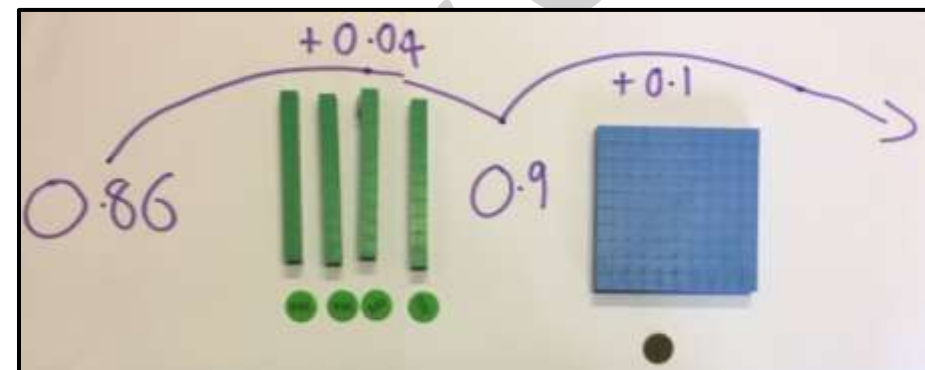
Using number facts
Derived facts from number bonds to 10 and 100, e.g. $2 - 0.45$ using $45 + 55 = 100$ or $3.00 - 0.86$ using $86 + 14 = 100$

Number bonds to £1, £10 and £100, e.g. $£4.00 - £3.86p = 14p$ or $£100 - £66$



Counting up to find the difference $1 - 0.86$

Applying number facts to decimals. $0.86 + 0.04 + 0.1 = 1$



Year 5 Written Subtraction

Expanded models consolidate place value up to 1 million in year 5. Similar models to be used with dienes blocks. The same model can be used to investigate subtraction of decimals

Compact column subtraction for numbers with up to 5 digits

$$\begin{array}{r} 01513114 \\ \times \quad \times \quad \times \quad \times \quad \times \\ - \quad 8 \quad 5 \quad 1 \quad 6 \\ \hline 7 \quad 8 \quad 0 \quad 8 \end{array}$$

Continue to use counting up subtraction for subtractions involving money, including finding change or, e.g. £50 - £28.76

$$\begin{array}{r} 24p \quad \quad \quad £1 \quad \quad \quad £20 \\ \hline £28.76 \quad £29 \quad \quad £30 \quad \quad \quad £50 \end{array}$$

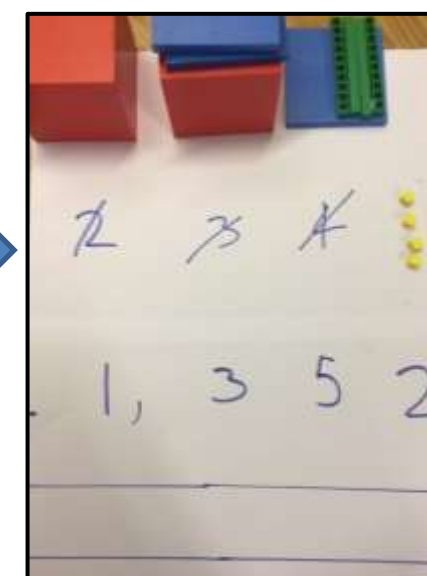
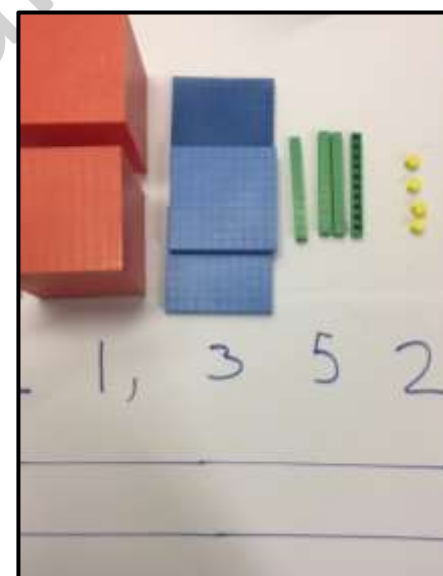
Use counting up subtraction to subtract decimal numbers, e.g. 4.2 - 1.74

$$\begin{array}{r} 0.06 \quad \quad 0.2 \quad \quad 2.2 \\ \hline 1.74 \quad 1.80 \quad \quad 2.0 \quad \quad \quad 4.2 \end{array}$$

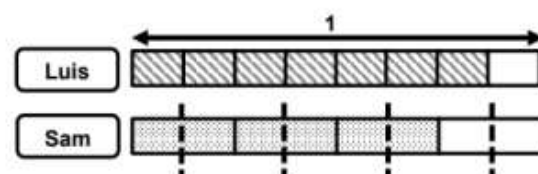
Subtracting fractions with like denominators, e.g. $1\frac{1}{8} - \frac{3}{8}$ as $1\frac{2}{8} - \frac{3}{8}$ or $\frac{10}{8} - \frac{3}{8} = \frac{7}{8}$



Using dienes to model column subtraction

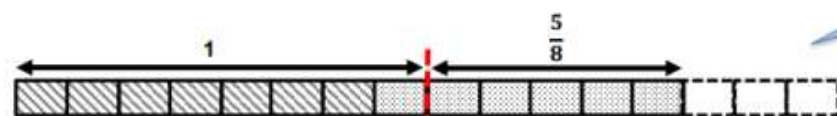


Sam and Luis have a pizza each. Sam eats $\frac{3}{4}$ of his pizza. Luis eats $\frac{7}{8}$ of his pizza. How much pizza have they eaten altogether?



$\frac{3}{4}$ is equivalent to $\frac{6}{8}$

How much pizza is left?



$$\frac{7}{8} + \frac{3}{4} = \frac{7}{8} + \frac{6}{8} = \frac{13}{8} = 1\frac{5}{8}$$

See addition page for concrete models of fractions for subtraction of fractions

Year 5 Mental Multiplication

Multiplication by partitioning

Multiplying and dividing by 10,100

Doubling and halving

Double amounts of money using partitioning, e.g. £6.73 doubled is double £6 (£12) plus double 73p (£1.46)

Use doubling and halving as a strategy in multiplying by 2, 4, 8, 5 and 20.

E.g. $58 \times 5 = \frac{1}{2} \text{ of } 58 (29) \times 10 (290)$

Grouping

Multiply decimals by 10, 100, 1000, e.g. $3.4 \times 100 = 340$

Use partitioning to multiply friendly 2-digit and 3-digit numbers by single-digit numbers.

E.g. 402×6 as $400 \times 6 (2400)$ and $2 \times 6 (12)$

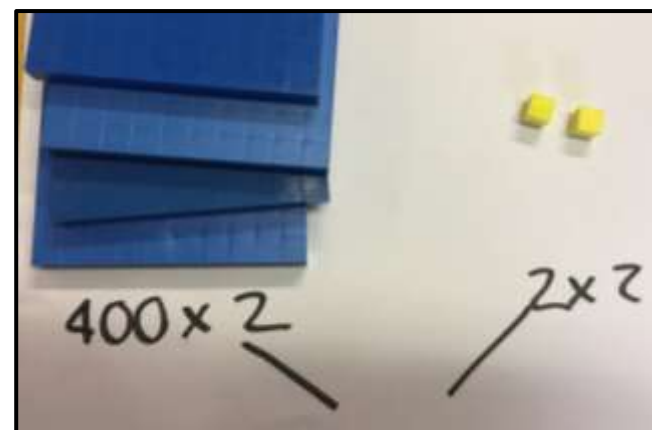
Use partitioning to multiply decimal numbers by single-digit numbers, e.g. 4.5×3 as $(4 \times 3) + (4 \times 0.5)$

Multiply using near multiples by rounding, e.g. 32×29 as $(32 \times 30) - 32$

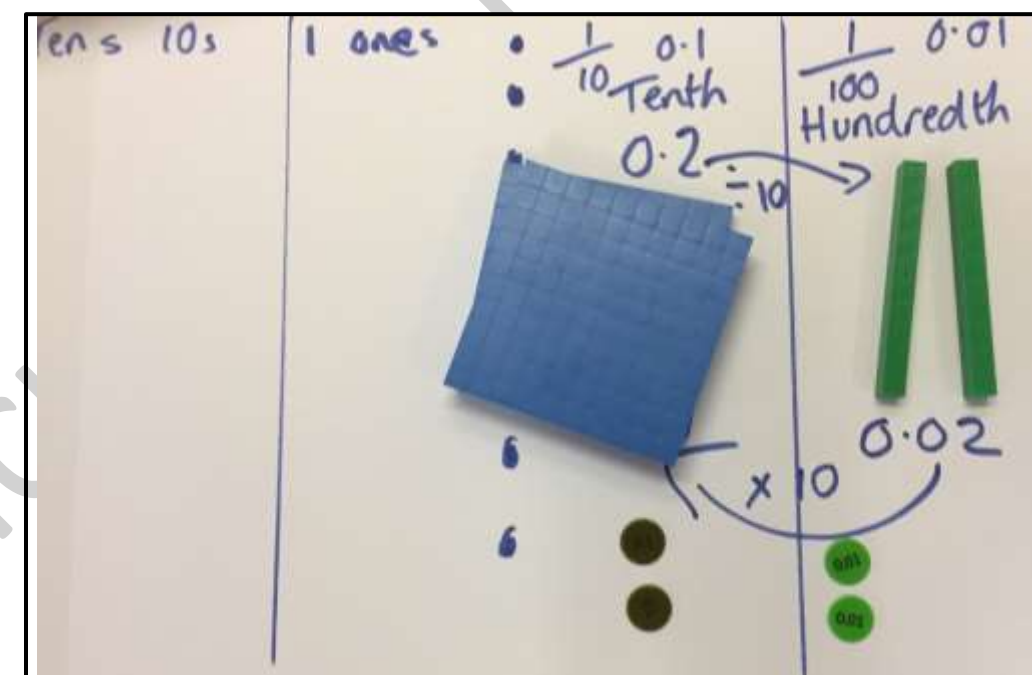
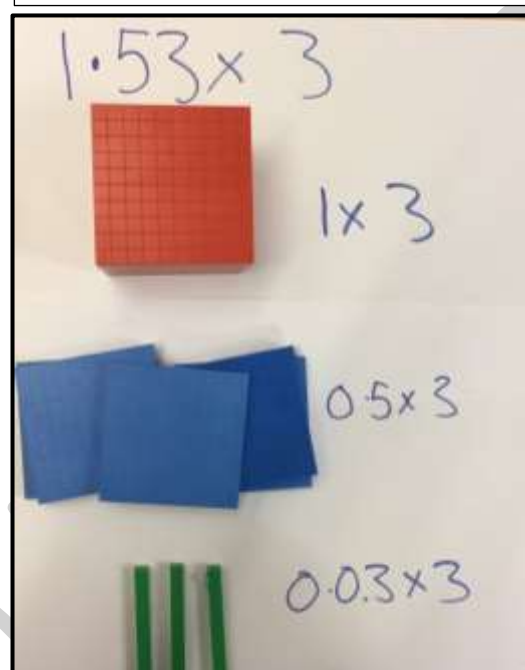
Using number facts

Use times tables facts up to 12×12 to multiply multiples of the multiplier, e.g. $4 \times 6 = 24$ so $40 \times 6 = 240$ and $400 \times 6 = 2400$

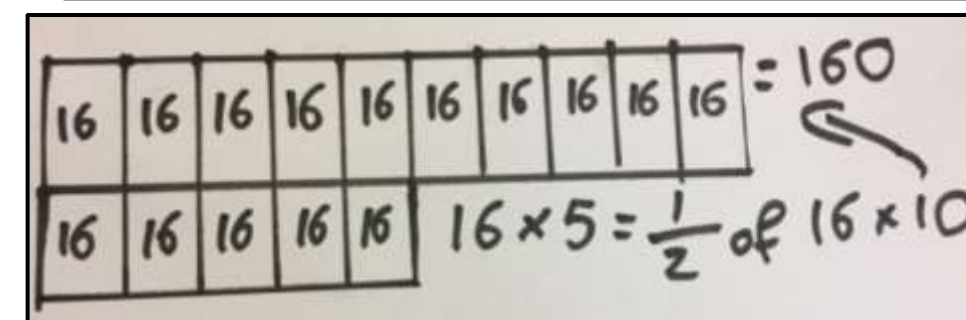
Know square numbers and cube numbers



Multiplying decimals by partitioning

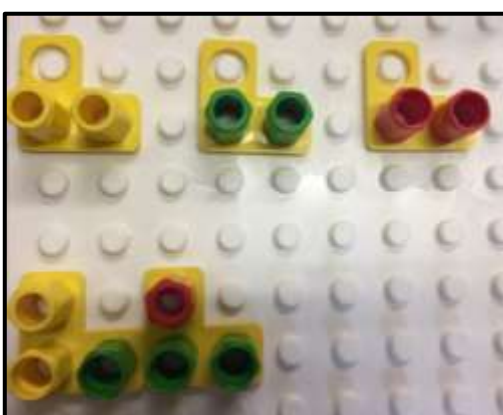


Multiplying by 5 by times 10 and halve

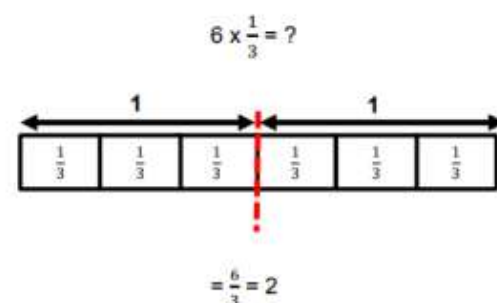


Using times tables facts and place value

2 100 000	700 000 x 3	70 000 x 30	7000 x 300	700 x 3000	70 x 30 000	7 x 300 000
210 000	70 000 x 3	7000 x 30	700 x 300	70 x 3000	7 x 30 000	
21 000	7000 x 3	700 x 30	70 x 300	7 x 3000		
2100	700 x 3	70 x 30	7 x 300			
210	70 x 3	7 x 30				
21	7 x 3					
2.1	0.7 x 3	7 x 0.3				
0.21	0.07 x 3	0.7 x 0.3	7 x 0.03			
0.021	0.007 x 3	0.07 x 0.3	0.7 x 0.03	7 x 0.003		



Two thirds x 3



How could you say this?
Refer the children back to the speaking frame.
Number of groups x size of each group = product.

Year 5 Written Multiplication

Use equipment to model short multiplication

Short multiplication of 2-digit, 3-digit and 4-digit numbers by 1-digit numbers

$$\begin{array}{r} 387 \\ \times 6 \\ \hline 54 \\ \hline 2322 \end{array}$$

Long multiplication of 2-digit, 3-digit and 4-digit numbers by teen numbers

Grid multiplication of numbers with up to 2 decimal places by single digit numbers

Multiplying fractions by single digit numbers
 E.g. $\frac{3}{4} \times 6 = \frac{18}{4}$ which is $4\frac{2}{4} = 4\frac{1}{2}$

Grid method taught alongside other multiplication methods provides an effective way of consolidating place value knowledge and developing fluency short and long algorithms

Long multiplication

$$\begin{array}{r}
 \times \quad 342 \\
 14 \\
 \hline
 1368 \\
 3420 \\
 \hline
 4788
 \end{array}$$

Base ten blocks representing the multiplication problems:

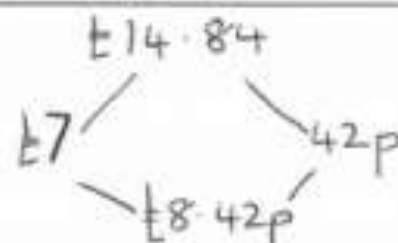
- 300×6 : Three hundred blocks (each labeled 100) and six blocks (each labeled 100).
- 80×6 : Eight blocks (each labeled 10) and six blocks (each labeled 10).
- 7×6 : Seven blocks (each labeled 1) and six blocks (each labeled 1).

	2	0.2	0.03
3			
3			
3			

Year 5 Mental division

Doubling and halving

Halve amounts of money using partitioning, e.g. half of £14.84 as half of £14 and half of 84p



Use doubling and halving as a strategy in dividing by 2, 4, 8, 5 and 20, e.g. $115 \div 5$ as double 115 (230) $\div 10$

Grouping

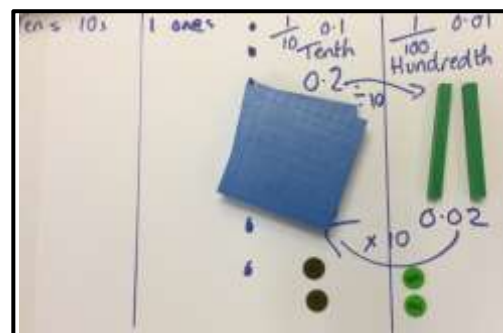
Divide numbers by 10, 100, 1000 to obtain decimal answers with up to three places, e.g. $340 \div 100 = 3.4$.

Use the 10th, 20th, 30th... multiple of the divisor to divide friendly 2-digit and 3-digit numbers by single-digit numbers, e.g. $186 \div 6$ as 30×6 (180) and 1×6 (6). Find unit & non-unit fractions of large amounts, e.g. $\frac{3}{5}$ of 265 is $3 \times (265 \div 5)$

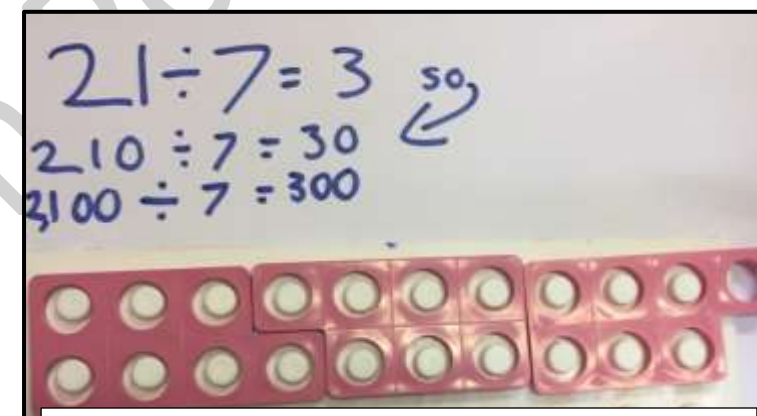
Using number facts

Use division facts from the times tables up to 12 x 12 to divide multiples of powers of ten of the divisor, e.g. $3600 \div 9$ using $36 \div 9$

Know square numbers and cube numbers

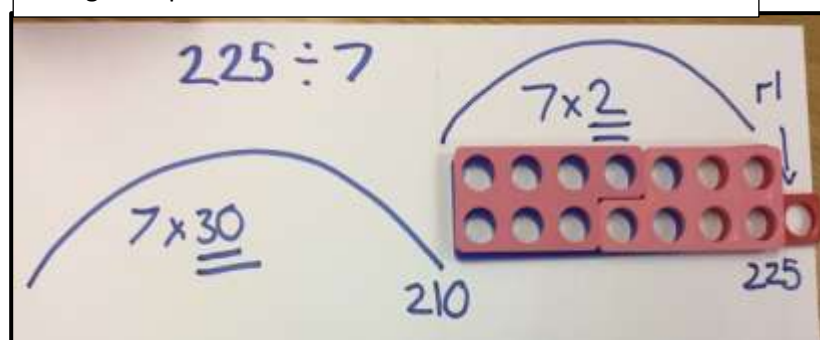


Dividing by 10 and 100



Using division facts and place value

Using multiples of ten of the divisor



Bar modelling division as grouping and sharing

Divide numbers ... interpret remainders appropriately for the context

The aim of these examples is to support understanding the bar model with remainders

Multiplication
Tracey put 4 seeds into each of her pots. She uses 6 pots and has 1 seed left over. How many seeds did she start with?

Why is the 'one' not in a block?

Grouping
Carl has 580 sweets. He wants to put 70 sweets in each bag. How many bags can he fill?

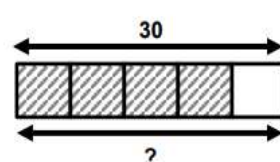
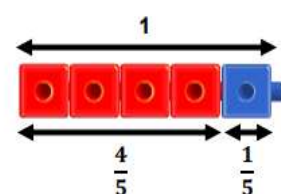
What does this number mean?
How many sweets would Carl have left for himself?
Carl has 20 sweets left.

Sharing
Grandad has been collecting his change in a jar. He has £9.15. He wants to share the money equally between seven grandchildren. How much money will each child receive?

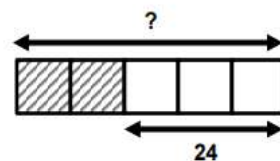
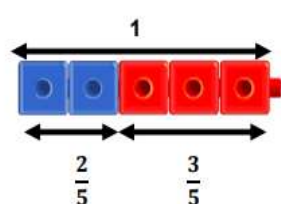
Why does the line have to include the remainder?

Find fractions of an amount using a bar model

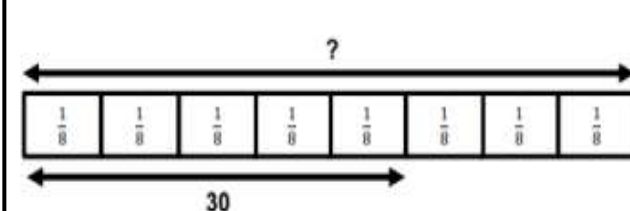
Sally buys four fifths of the shop's apples. If the shop had 30 apples, how many apples did she buy?



James had some football cards. He gave two fifths away. He now has 24 cards. How many did he have to start with?

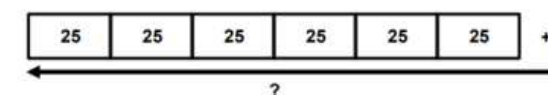


30 is $\frac{2}{5}$ of a number. What is the number?

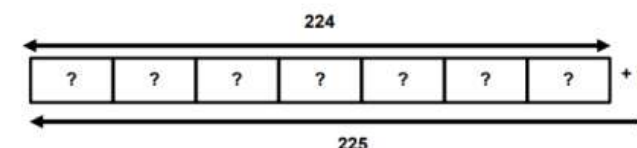


Deeper understanding of division

$$\square \div 6 = 25 \text{ r } 4$$



$$225 \div \square = 7 \text{ r } 1$$



Year 5 Written division

Mental strategy of division linked to written version. 'How many 6s in 326?'

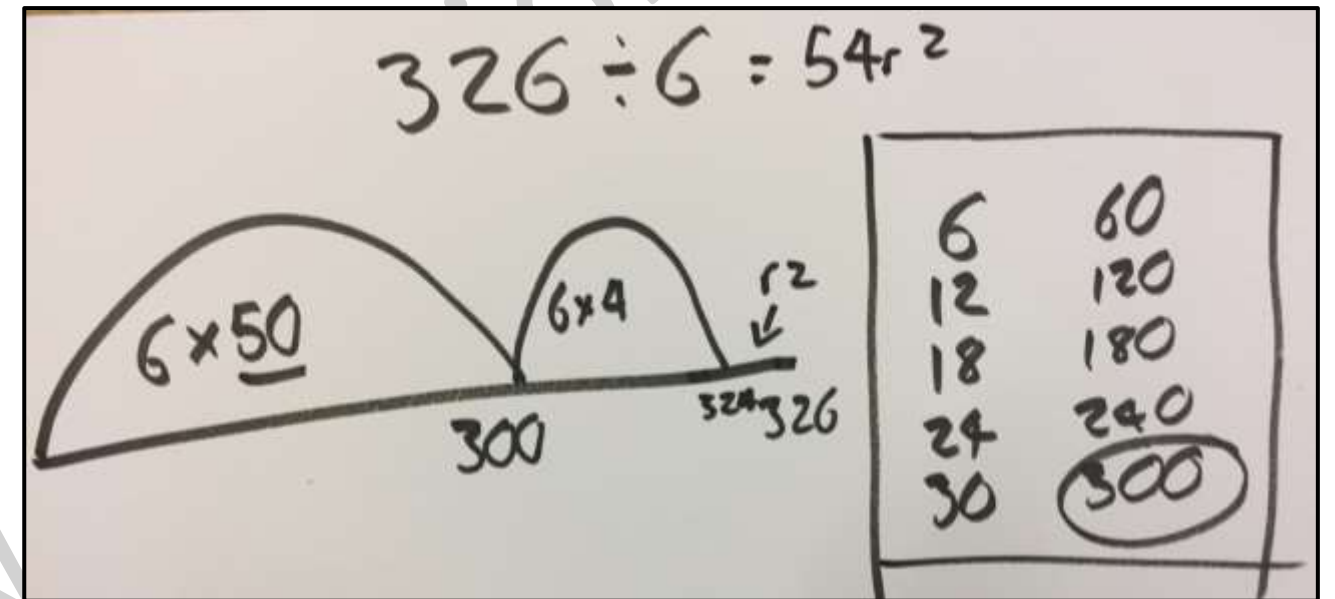
Written version of a mental strategy for 3-digit \div 1 digit numbers

Short division of 3-digit and 4-digit numbers by single-digit numbers

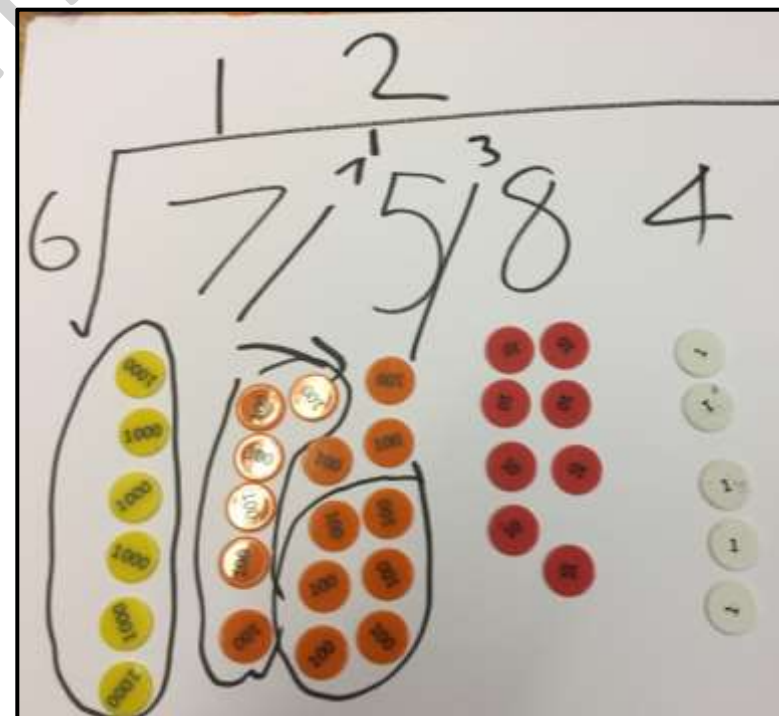
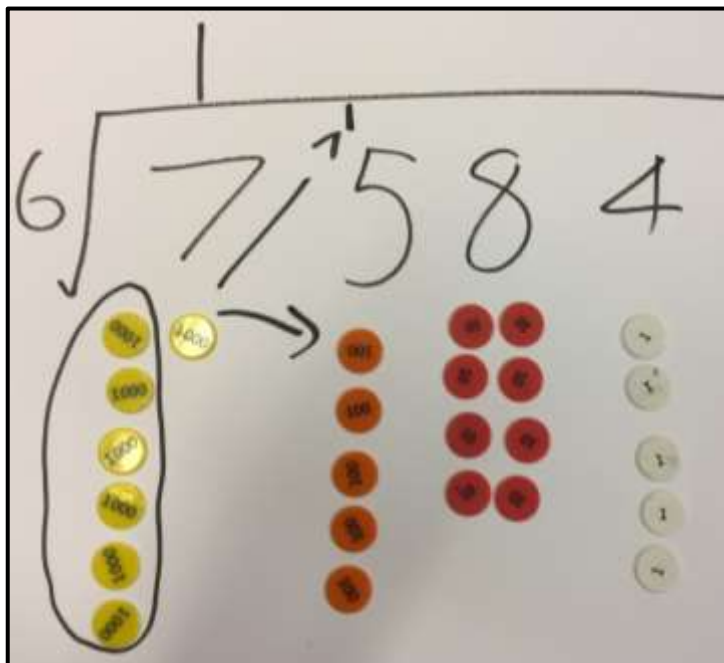
$$\begin{array}{r} 1264 \\ 6 \overline{) 71584} \end{array}$$

$$\begin{array}{l} \square \times 6 = 326 \\ 50 \times 6 = 300 \\ 26 \\ 4 \times 6 = 24 \\ 2 \\ 54 \text{ r}2 \end{array}$$

$$326 \div 6 = 54 \text{ r}2$$



Grouping and exchanging of counters helps to model short division



Year 6 Mental Addition

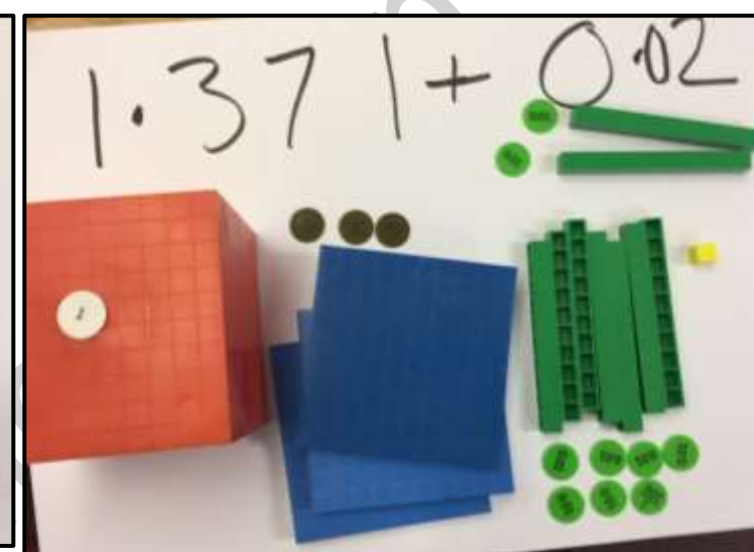
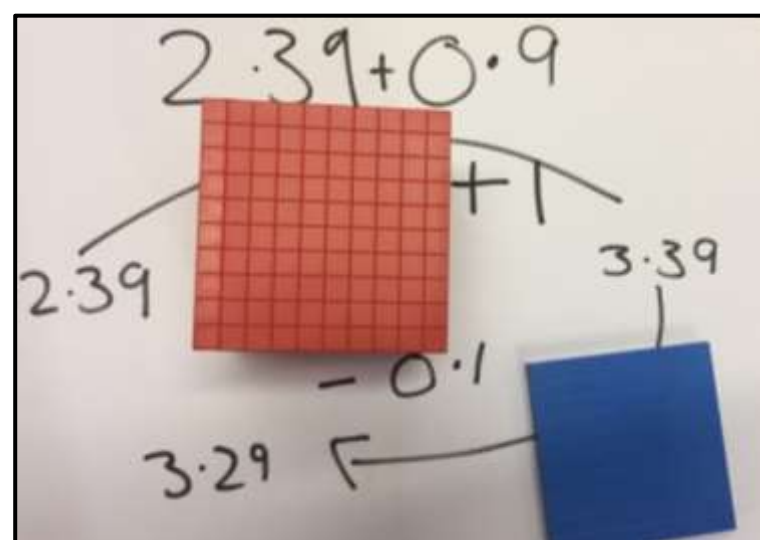
Revision of addition strategies from year 5 up to 3 decimal places

Using Place value
Count in 0.1s, 0.01s, 0.001s, e.g. knowing what 0.001 more than 6.725 is
Partitioning, e.g. $9.54 + 3.25$ as $9 + 3$ and $0.5 + 0.2$ and $0.04 + 0.05$ to get 12.79

100s	10s	1s	0.1s	0.01s	0.001s
		6	7	2	5
		0	0	0	1
		6	7	2	6

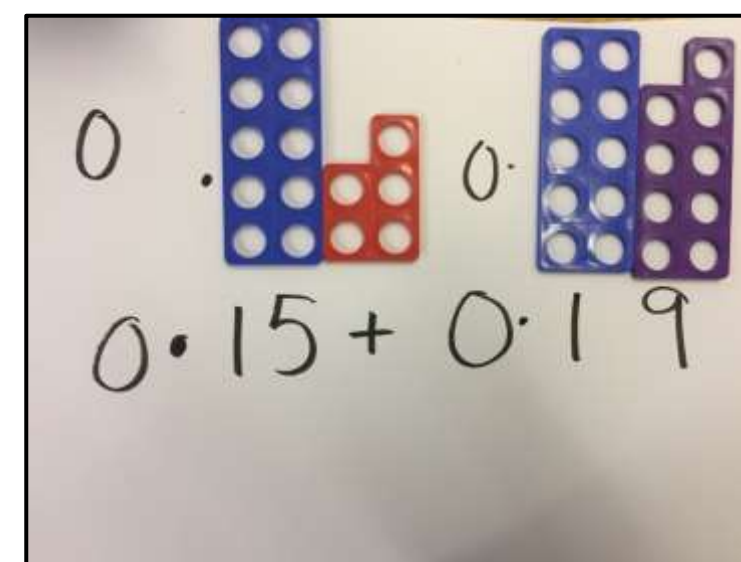
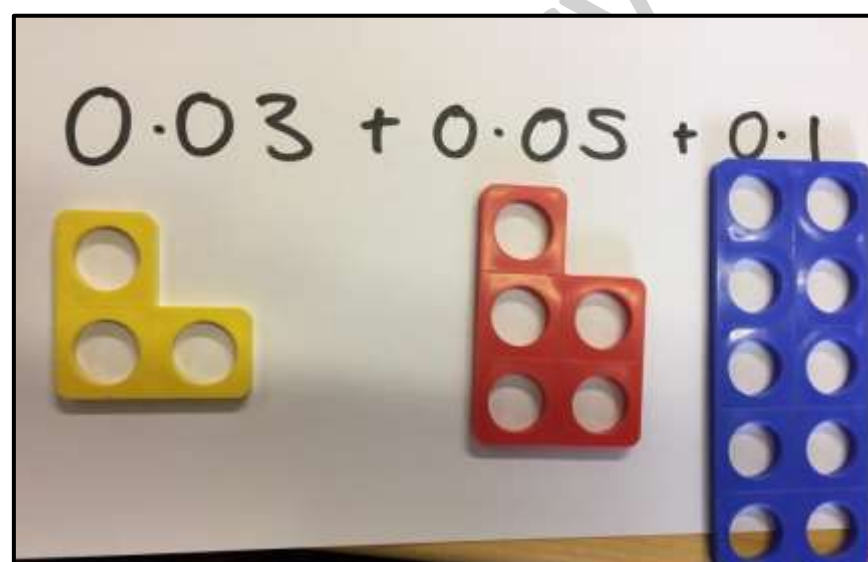
Counting on
Add two decimal numbers by adding the ones then the tenths/hundredths or thousandths, e.g. $6.314 + 3.006$ as 6.314 add 3 (9.314) then add 0.006 (9.32)
Add near multiples of 1, e.g. $6.345 + 0.999$ or $5.673 + 0.9$
Count on from large numbers, e.g. $16,375 + 12,003$

Using number facts
Number bonds to 1 and to next multiple of 1, e.g. $0.63 + 0.37$ or $2.355 + 0.645$
Add to next ten, e.g. $4.62 + 0.38$



Revising of number facts with decimals

$0.05 + 0.05$ does not = 0.010



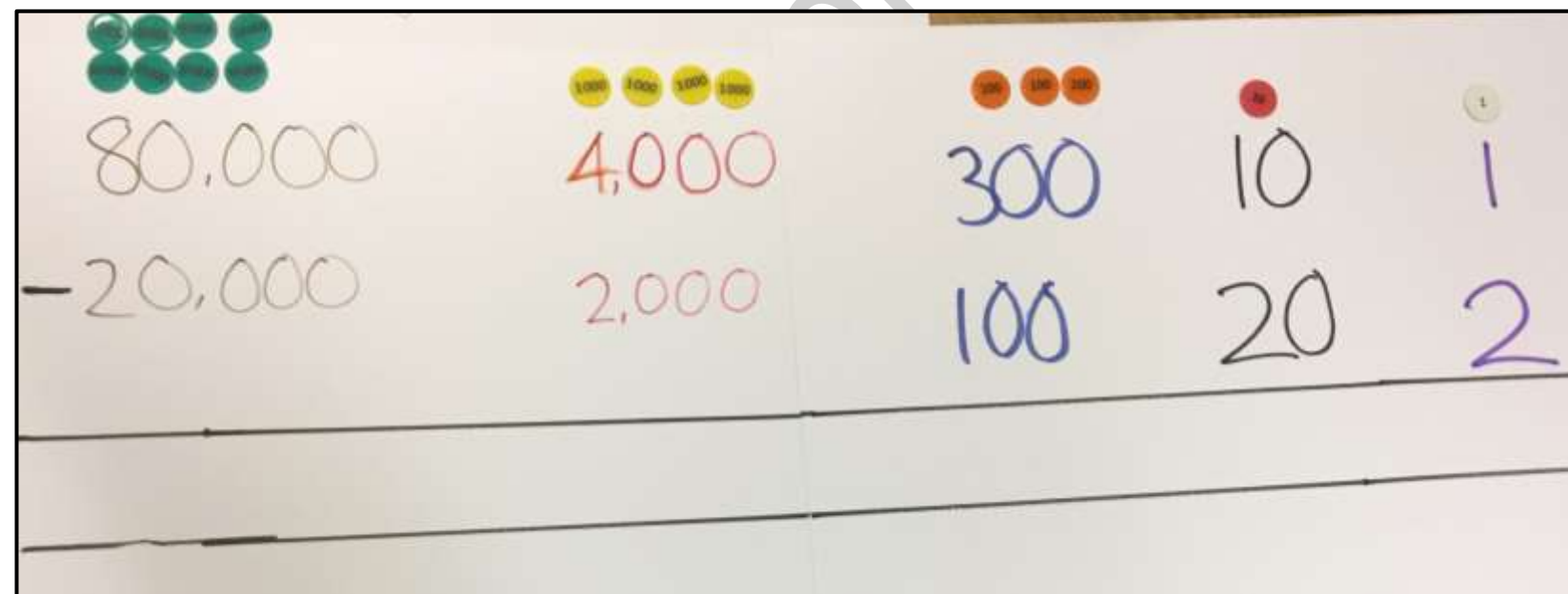
Year 6 Written Addition

Compact column addition
for adding several large numbers
and decimal numbers with up
to two places

$$\begin{array}{r} £14.64 \\ + £28.78 \\ + £12.26 \\ \hline 11.1 \\ \hline £55.68 \end{array}$$

Compact column addition with
money

Add fractions with unlike denominators, e.g. $\frac{1}{2} + \frac{1}{3} = 1 \frac{1}{12}$ or $\frac{13}{12}$
 $2 \frac{1}{4} + 1 \frac{1}{3} = 3 \frac{7}{12}$



Expanded model helps to consolidate place value up to 10 million in year 6. The same model can be used to investigate addition of decimals

Adding fractions with different denominators

• $\frac{1}{2} + \frac{1}{4} = ?$

In order to be able to add these fractions, the children need to convert them into equivalent fractions. Using Cuisenaire rods can support them in refreshing their knowledge of equivalent fractions.

The purple rod has been selected as this will allow the children to see one half and one quarter on the same model

If purple is the whole, what colour shows us half? (red)
What colour rod would show us quarters?
Can we rename half? Yes, two quarters.

$\frac{1}{2} + \frac{1}{4} = \frac{1}{4} + \frac{1}{4} + \frac{1}{4} = \frac{3}{4}$

Deepen understanding by asking the children if there are other colour rods which would allow us to show halves and quarters on the same model.

$\frac{1}{2} + \frac{1}{4} = \frac{1}{4} + \frac{1}{4} + \frac{1}{4} = \frac{3}{4}$

• $\frac{1}{2} + \frac{1}{3} = ?$

Which colour rods will allow us to represent halves and thirds on the same model?
Can you explain why?
If the children need to allow them to explore.

$\frac{1}{2} + \frac{1}{3} = \frac{3}{6} + \frac{2}{6} = \frac{5}{6}$

$\frac{1}{3} + \frac{2}{5}$ cannot be added as the denominators are different.

$\frac{5}{15} + \frac{6}{15}$

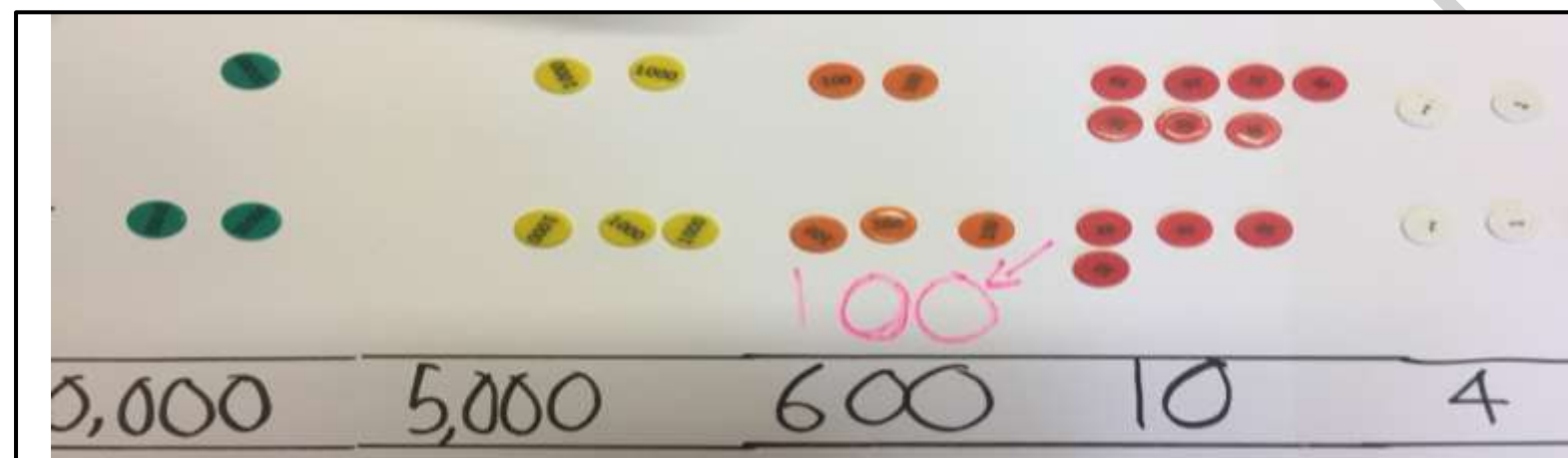
Year 6 subtraction

Taking away
Use place value to subtract decimals, e.g. $7.782 - 0.08$ or $16.263 - 0.2$, etc.
Take away multiples of powers of 10, e.g. $132,956 - 400$ or $686,109 - 40,000$ or $7.823 - 0.5$
Partition or count back, e.g. $3964 - 1051$ or $5.72 - 2.01$
Subtract near multiples, e.g. $360,078 - 99,998$ or $12.831 - 0.99$

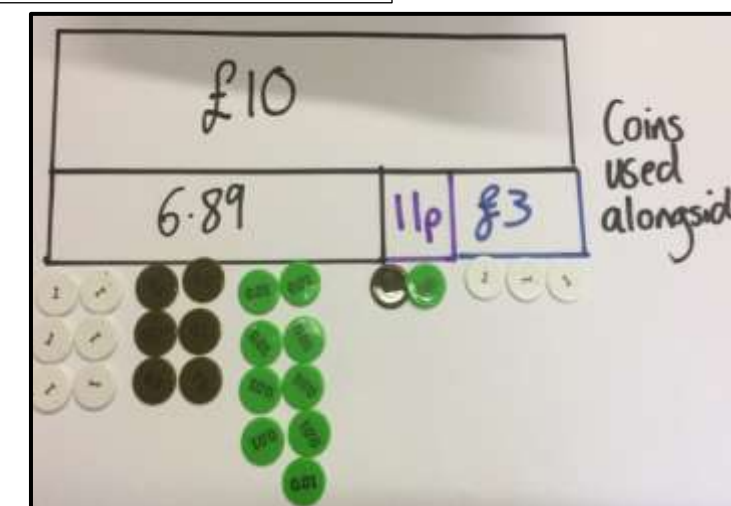
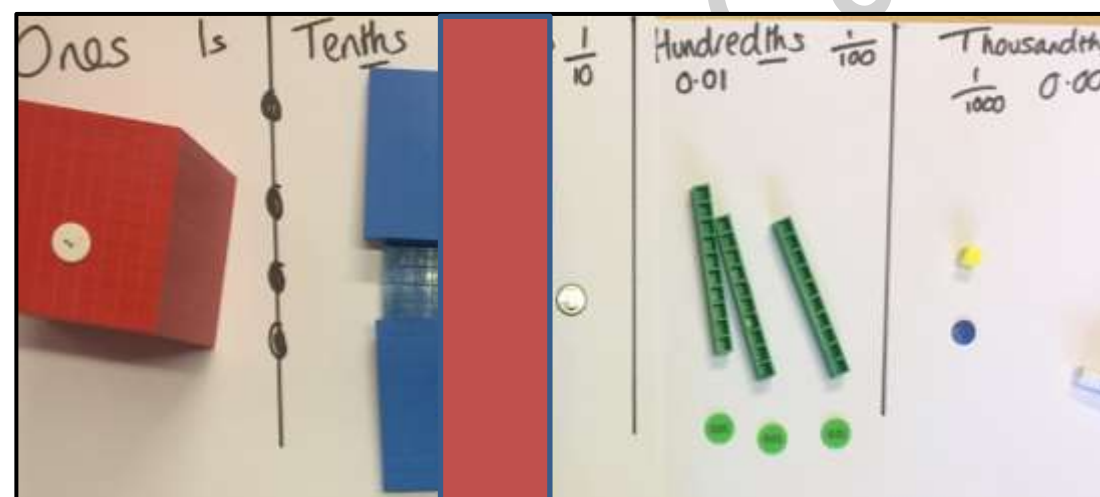
Counting up
Count up to subtract numbers from multiples of 10, 100, 1000, 10,000
Find a difference between two decimal numbers by counting up from the smaller to the larger, e.g. $1.2 - 0.87$

Using number facts
Derived facts from number bonds to 10 and 100, e.g. $0.1 - 0.075$ using $75 + 25 = 100$ or $5 - 0.65$ using $65 + 35 = 100$

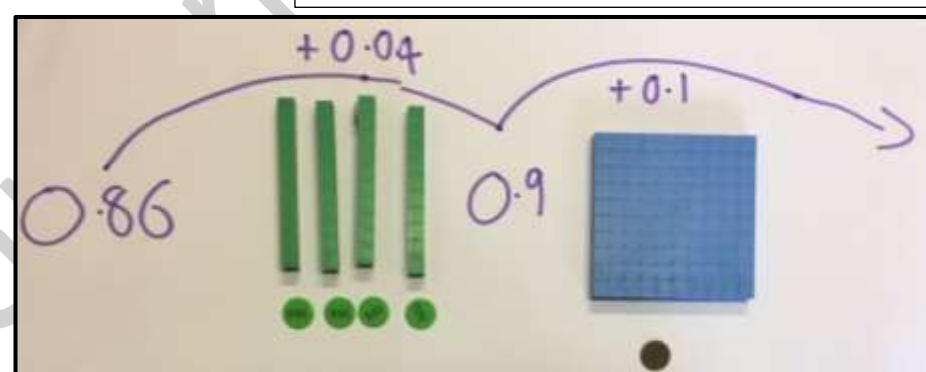
Number bonds to £1, £10 and £100, e.g. $£7.00 - £4.37$ or $£100 - £66.20$ using $20p + 80p = £1$ and $£67 + £33 = £100$.



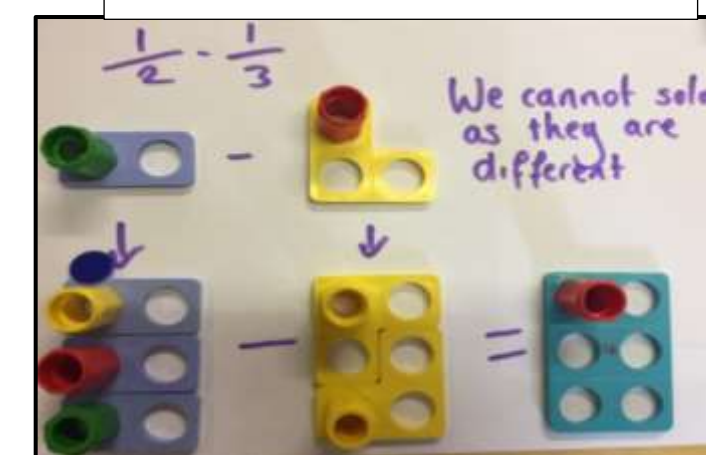
Expanded model helps to consolidate place value up to 10 million in year 6. The same model can be used to investigate subtraction of decimals



Revision of subtraction strategies from year 5 with numbers up to 10 million and 3dp



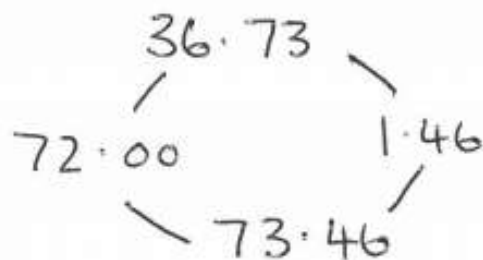
Subtraction of fractions with different denominators



Year 6 Multiplication

Doubling and halving

Double decimal numbers with up to 2-places using partitioning, e.g. 36.73 doubled is double 36 (72) plus double 0.73 (1.46)



Use doubling and halving as strategies in mental multiplication

Grouping

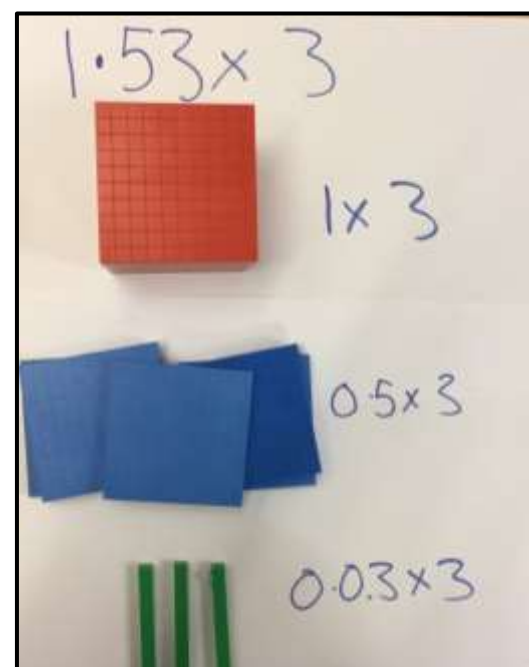
Use partitioning as a strategy in mental multiplication, as appropriate, e.g. 3060×4 as $(3000 \times 4) + (60 \times 4)$ or 8.4×8 as 8×8 (64) and 0.4×8 (3.2)

Use factors in mental multiplication, e.g. 421×6 as 421×3 (1263) doubled (2526) or 3.42×5 as half of (3.42×10)

Using number facts

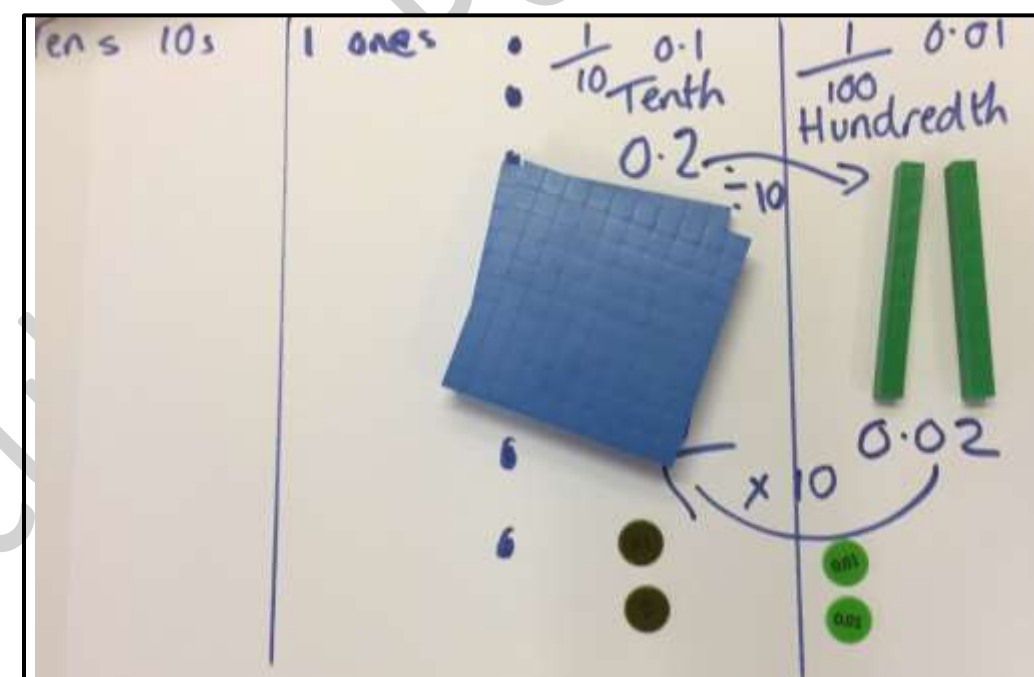
Use times tables facts up to 12×12 in mental multiplication of large numbers or numbers with up to two decimal places, e.g. $6 \times 4 = 24$ and $0.06 \times 4 = 0.24$

Multiplication of decimals by partitioning



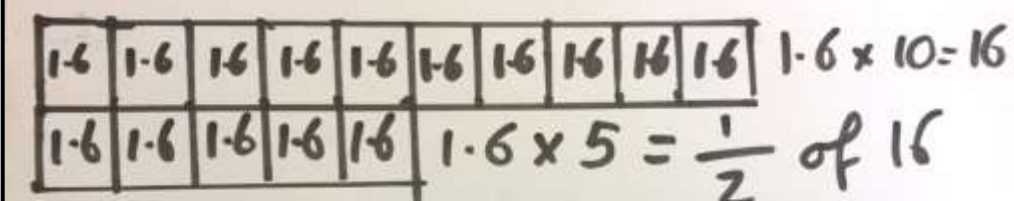
Double 0.59

Multiplication of numbers by 10,100,1000

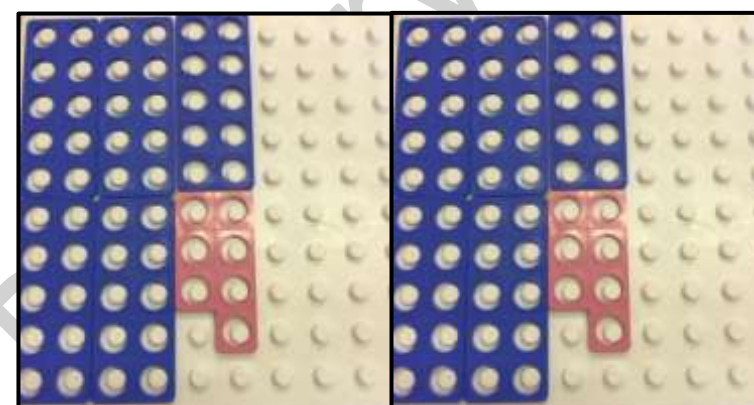
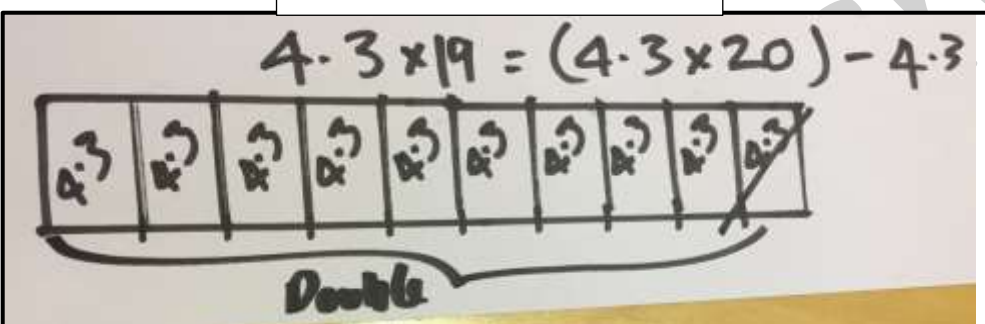


Linking place value and number facts

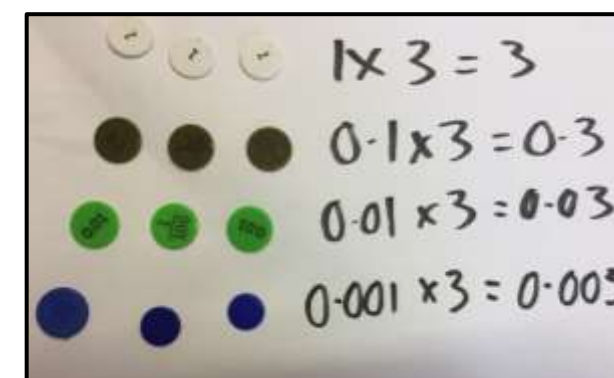
X 5 = X10 the halve



X19 = x20 then - one group



Linking place value and number facts



2 100 000	700 000 x 3	70 000 x 30	7000 x 300	700 x 3000	70 x 30 000	7 x 300 000
210 000	70 000 x 3	7000 x 30	700 x 300	70 x 3000	7 x 30 000	
21 000	7000 x 3	700 x 30	70 x 300	7 x 3000		
2100	700 x 3	70 x 30	7 x 300			
210	70 x 3	7 x 30				
21	7 x 3					
2.1	0.7 x 3	7 x 0.3				
0.21	0.07 x 3	0.7 x 0.3	7 x 0.03			
0.021	0.007 x 3	0.07 x 0.3	0.7 x 0.03	7 x 0.003		

Year 6 Written Multiplication

Short multiplication of 2-digit, 3-digit and 4-digit numbers by 1-digit numbers

$$\begin{array}{r} 3875 \\ \times 6 \\ \hline 543 \\ \hline 23250 \end{array}$$

Long multiplication of 2-digit, 3-digit and 4-digit numbers by 2-digit numbers

Short multiplication of decimal numbers using $\times 100$ and $\div 100$, e.g. 13.72×6 as $1372 \times 6 \div 100$

Short multiplication of money, $\pounds 13.72 \times 6$

Grid multiplication of numbers with up to 2 decimal places by single digit numbers

Multiplying proper and improper fractions, e.g. $\frac{3}{4} \times \frac{2}{3}$

NB Grid multiplication provides a default method for ALL children

$$\begin{array}{r} \times 342 \\ 1368 \\ 3420 \\ \hline 4788 \end{array}$$

$$\begin{array}{r} 300 \times 6 \\ 80 \times 6 \\ 7 \times 6 \\ \hline \end{array}$$

\times	2	0.2	0.03
3	6	0.6	0.09

When multiplying fractions by fractions, it is crucial that learners understand \times as (lots) of

• $1 \times \frac{1}{4} =$

How can I show $\frac{1}{4}$ of the purple rod?

Why have I selected the purple rod? What value does it represent?

• $3 \times \frac{1}{4} =$

If purple represents one, how many do I need?

So what is the answer?

• $\frac{1}{2} \times \frac{1}{2} =$

If purple equals the whole... What is half?

So white is equivalent to one half of the group of a half. But what is its value?

In order to find the value of white, the children need to refer back to the whole.

White is one quarter

• $\frac{1}{4} \times \frac{1}{2} =$

In this case, we need to discover how big one quarter group of one half is.

Where is one quarter of one half?

What is its value? $\frac{1}{8}$

What is one half of one quarter? (application of commutativity)

$\frac{1}{2} \times \frac{1}{2} = \frac{1}{4}$

$\frac{1}{4} \times \frac{1}{2} = \frac{1}{8}$

$\times \frac{1}{2}$

I cannot find $\frac{1}{2}$ of $\frac{1}{5}$ so change representation

$\times \frac{1}{2} =$

Year 6 Division

Revising division methods from year 5

Doubling and halving
Halve decimal numbers with up to 2-places using partitioning, e.g. half of 36.86 is half of 36 (18) plus half of 0.86 (0.43)

Use doubling and halving as strategies in mental division, e.g. $216 \div 4$ is half of 216 (108) and half of 108 (54)

Grouping
Use 10^m , 20^m , 30^m , ... or 100^m , 200^m , 300^m , ... multiples of the divisor to divide large numbers, e.g. $378 \div 9$ as $40 \times 9 = 360$ and $2 \times 9 = 18$ so the answer is 42
Use tests for divisibility, e.g. 135 divides by 3 as $1 + 3 + 5 = 9$ and 9 is in the 3x table

Using number facts
Use division facts from the times tables up to 12×12 to divide decimal numbers by single-digit numbers, e.g. $1.17 \div 3$ is $\frac{1}{100}$ of $117 \div 3$ (0.39)

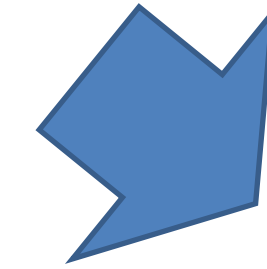
Short division of 3-digit and 4-digit numbers by single-digit numbers

Long division of 3-digit and 4-digit numbers by two-digit numbers

Divide fractions by whole numbers

Long division. Note: Multiples of divisor on the right hand side

Long division. Note: Multiples of divisor on the right hand side



$326 \div 6 = 54r2$

Handwritten diagram showing the division process using a number line and a multiplication table.

6	60
12	120
18	180
24	240
30	300

Handwritten diagram showing the division process using a number line and a multiplication table.

Handwritten diagram showing the division process using a number line and a multiplication table.

$\frac{1}{3} \div 3 =$

If you share _____ equally between _____ groups, how many are there in each group?

What else can you see?

I can see that $\frac{1}{3}$ is $\frac{1}{3}$ of $\frac{1}{3}$.

I can see that $3 \times \frac{1}{3}$ is equal to $\frac{3}{3}$.

I can see how many fifths are in three fifths.

$\frac{1}{3} \div 2 =$

What else can you see?

I can see that half of one third is one sixth.

I can see double one sixth is equal to one third.

I can see two sixths are equivalent to one third.

I can see that there are two sixths in a third.

Division of fractions by whole numbers

Handwritten diagram showing the division process using a number line and a multiplication table.